

# An introduction to R: a short course

## Part II

Multivariate analysis

# The zelig website

## ZELIG: EVERYONE'S STATISTICAL SOFTWARE

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**Version:3.4-5** ([Download](#)) ([What's new](#))



Zelig is named after a Woody Allen movie about a man who had the strange ability to become the physical and psychological reflection of anyone he met and thus to fit perfectly in any situation.

Zelig is a single, easy-to-use program that can estimate, help interpret, and present the results of a large range of statistical methods. It literally *is* "everyone's statistical software" because Zelig uses [\(R\)](#) code from many researchers. We also hope it will *become* "everyone's statistical software" for applications, and we have designed it so that anyone can use it or add their methods to it. Zelig comes with detailed, self-contained documentation that minimizes startup costs for Zelig and R, automates graphics and summaries for all models, and, with only three simple commands required, generally makes the power of R accessible for all users. Zelig also works well for teaching, and is designed so that scholars can use the same program with students that they use for their research.

Zelig adds considerable infrastructure to improve the use of existing methods. It generalizes the program [Clarify](#) (for Stata), which translates hard-to-interpret coefficients into quantities of interest; combines multiply imputed data sets (such as output from [Amelia](#)) to deal with missing data; automates bootstrapping for all models; uses sophisticated nonparametric matching commands which improve parametric procedures (via [MatchIt](#)); allows one-line commands to run analyses in all designated strata; automates the creation of replication data files so that you (or, if you wish, anyone else) can replicate the results of your analyses (hence satisfying the [replication standard](#)); makes it easy to evaluate counterfactuals (via [WhatIf](#)); and allows conditional population and superpopulation inferences. Zelig includes many specific methods, based on likelihood, frequentist, Bayesian, robust Bayesian, and nonparametric theories of inference.

- [Documentation](#) and [Installation](#)
- [Installation](#), [Frequently Asked Questions](#)
- Please send **All** questions, bugs and requests: Zelig Mailing List, [\[Un\]Subscribe](#), or [Browse/Search Archives](#)
- A paper that describes the advances underlying Zelig software: Kosuke Imai, Gary King, and Olivia Lau. "**Toward A Common Framework for Statistical Analysis and Development**" *Journal of Computational and Graphical Statistics*, Vol. 17, No. 4 (December), pp. 892-913 ([Abstract: HTML](#) | [Paper: PDF](#))
- [Slides used to introduce Zelig](#)
- [Be notified of Zelig changes](#)

<http://gking.harvard.edu/zelig/>

# Multivariate analysis

- I. Dimension reduction through factor analysis, principal components analysis, cluster analysis, and multidimensional scaling
- II. Multiple measures of reliability
- III. Practical use of R for scoring inventories

# Dimension Reduction

- I. The problem: How best to summarize and think about many variables some of which are moderately correlated
- II. The solutions: rank reduction through FA, PCA, CA, MDS
- III.Examples will be tests and then items

# The Thurstone data set

```
> data(bifactor)
> colnames(Thurstone) <- c
("Sentences", "Vocab", "S.comp", "F.letter", "4.letter", "Suffix",
 "Series", "Pedi", "letters")

> round(Thurstone, 2)
```

	Sentences	Vocab	S.comp	F.letter	4.letter	Suffix	Series	Pedi	letters
Sentences	1.00	0.83	0.78	0.44	0.43	0.45	0.45	0.54	0.38
Vocabulary	0.83	1.00	0.78	0.49	0.46	0.49	0.43	0.54	0.36
Sent.Completion	0.78	0.78	1.00	0.46	0.42	0.44	0.40	0.53	0.36
First.Letters	0.44	0.49	0.46	1.00	0.67	0.59	0.38	0.35	0.42
4.Letter.Words	0.43	0.46	0.42	0.67	1.00	0.54	0.40	0.37	0.45
Suffixes	0.45	0.49	0.44	0.59	0.54	1.00	0.29	0.32	0.32
Letter.Series	0.45	0.43	0.40	0.38	0.40	0.29	1.00	0.56	0.60
Pedigrees	0.54	0.54	0.53	0.35	0.37	0.32	0.56	1.00	0.45
Letter.Group	0.38	0.36	0.36	0.42	0.45	0.32	0.60	0.45	1.00

# How many dimensions

I. Chi Square test

II. Scree plot

III. Parallel analysis of random data

IV. Minimum Average Partial correlation

V. Very Simple Structure

VI. Do not use eigen value > 1 rule!

```
> factanal(covmat=Thurstone,factors=3,n.obs =213)
Call:
factanal(factors = 3, covmat = Thurstone, n.obs = 213)
Uniquenesses:
```

Sentences	Vocab	S.comp	F.letter	4.letter	Suffix	Series
Pedi	letters					
0.175	0.165	0.268	0.268	0.372	0.504	0.282
0.496	0.473					

Loadings:

	Factor1	Factor2	Factor3
Sentences	0.834	0.244	0.264
Vocabulary	0.827	0.318	0.223
Sent.Completion	0.775	0.284	0.227
First.Letters	0.228	0.792	0.230
4.Letter.Words	0.213	0.706	0.291
Suffixes	0.314	0.616	0.134
Letter.Series	0.232	0.179	0.795
Pedigrees	0.446	0.166	0.527
Letter.Group	0.154	0.311	0.638

	Factor1	Factor2	Factor3
SS loadings	2.454	1.902	1.642
Proportion Var	0.273	0.211	0.182
Cumulative Var	0.273	0.484	0.666

Test of the hypothesis that 3 factors are sufficient.

The chi square statistic is 2.82 on 12 degrees of freedom.

The p-value is 0.997

MLE  
factor  
analysis:  
factanal

Call:

```
factanal(factors = 2, covmat = Thurstone, n.obs = 213)
```

Uniquenesses:

Sentences	Vocab	S.comp	F.letter	4.letter	Suffix	Series
Pedi	letters					
0.168	0.178	0.269	0.322	0.344	0.537	0.680
0.612	0.677					

Loadings:

	Factor1	Factor2
Sentences	0.866	0.287
Vocabulary	0.839	0.343
Sent.Completion	0.795	0.314
First.Letters	0.255	0.783
4.Letter.Words	0.235	0.775
Suffixes	0.317	0.602
Letter.Series	0.372	0.426
Pedigrees	0.524	0.336
Letter.Group	0.269	0.501

	Factor1	Factor2
SS loadings	2.793	2.420
Proportion Var	0.310	0.269
Cumulative Var	0.310	0.579

Test of the hypothesis that 2 factors are sufficient.

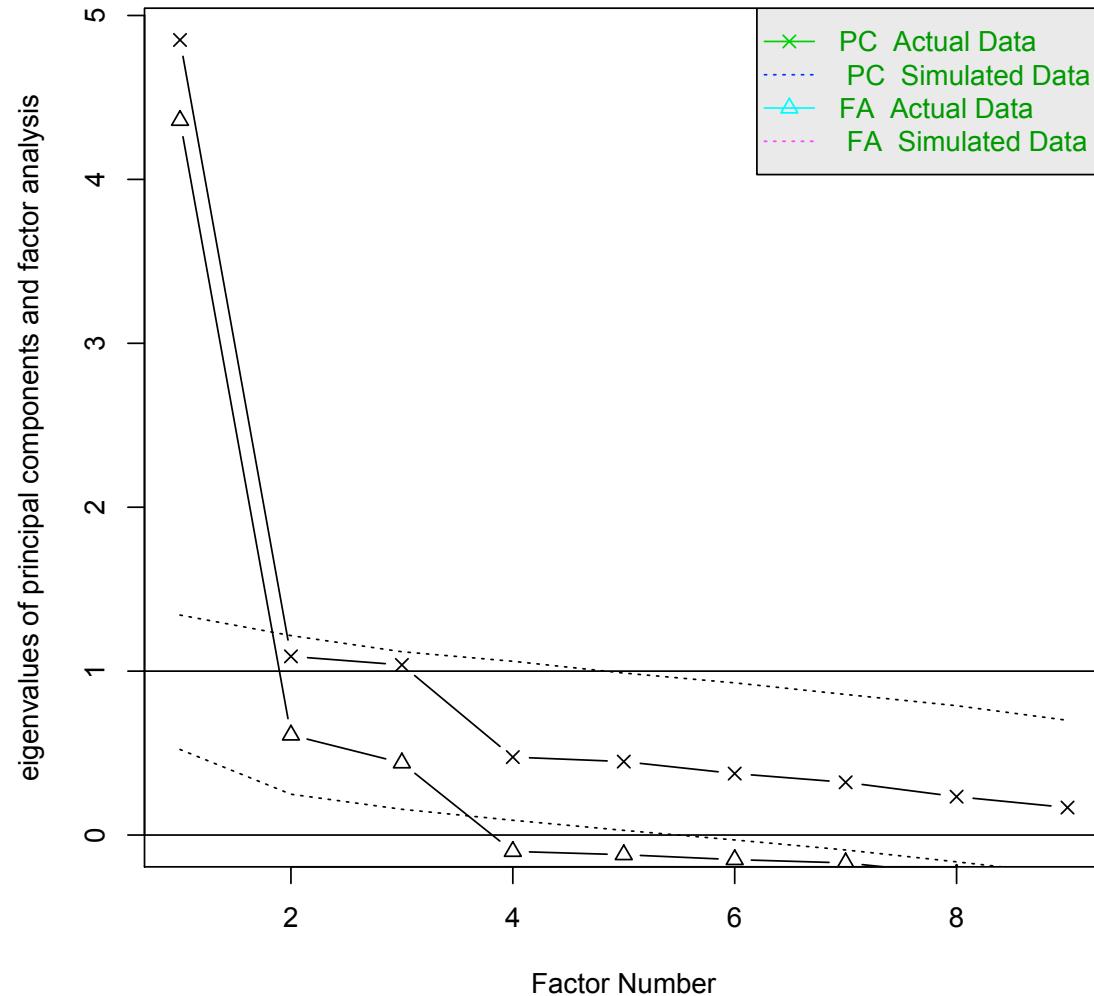
The chi square statistic is 82.84 on 19 degrees of freedom.

The p-value is 5.99e-10

chi square  
rejects a 2  
factor  
solution

# Parallel analysis

Parallel Analysis Scree Plots



# Very Simple Structure and MAP

```
> vss <- VSS(Thurstone, n.obs=213, SMC=FALSE)
> vss
```

Very Simple Structure

Call: VSS(x = Thurstone, n.obs = 213, SMC = FALSE)

VSS complexity 1 achieves a maximum of 0.88 with 1 factors

VSS complexity 2 achieves a maximum of 0.92 with 2 factors

The Velicer MAP criterion achieves a minimum of 1 with 3 factors

Velicer MAP

```
[1] 0.07 0.07 0.07 0.11 0.20 0.31 0.59 1.00
```

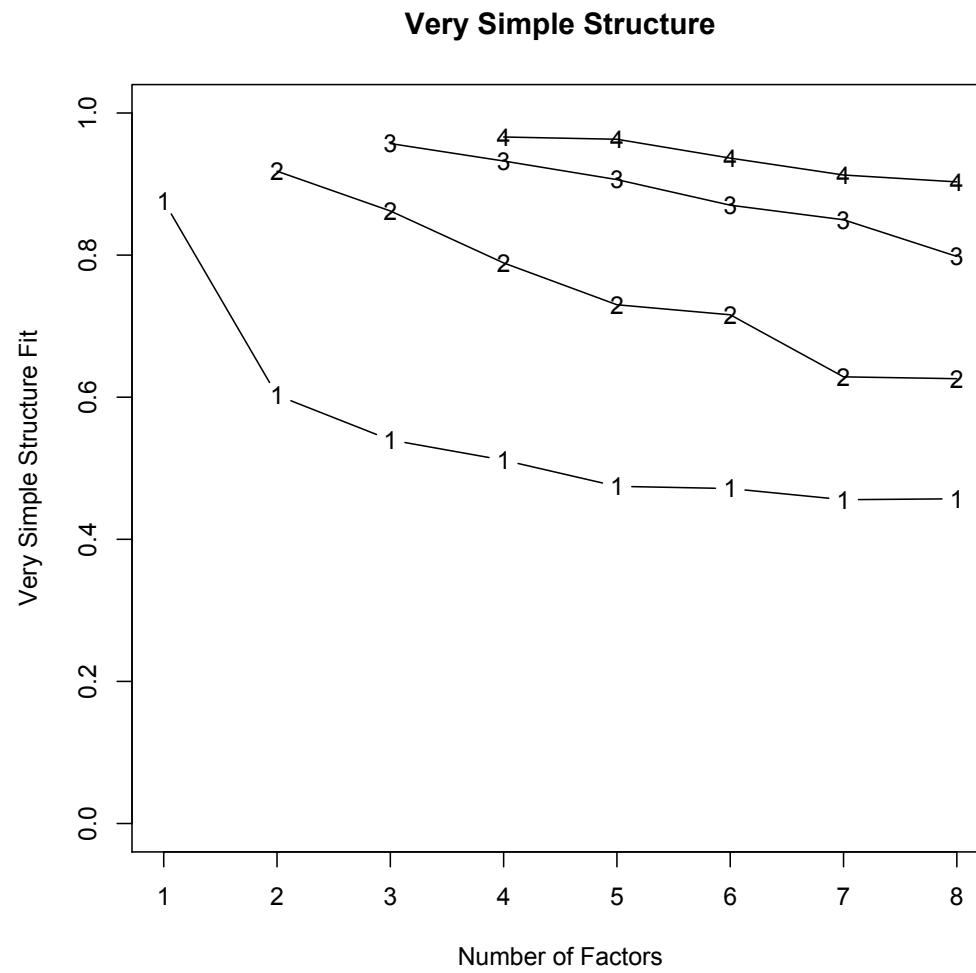
Very Simple Structure Complexity 1

```
[1] 0.88 0.60 0.54 0.51 0.47 0.47 0.46 0.46
```

Very Simple Structure Complexity 2

```
[1] 0.00 0.92 0.86 0.79 0.73 0.72 0.63 0.63
```

# Very Simple Structure



# Principal Axis FA

```
> pa3 <- factor.pa(Thurstone,nfactors=3,n.obs=213)
> pa3
```

	V	PA1	PA2	PA3
Sentences	1	0.83		
Vocab	2	0.83	0.32	
S.comp	3	0.78		
F.letter	4		0.79	
4.letter	5		0.71	
Suffix	6	0.31	0.62	
Series	7			0.79
Pedi	8	0.45		0.53
letters	9		0.31	0.64

	PA1	PA2	PA3
SS loadings	2.46	1.91	1.64
Proportion Var	0.27	0.21	0.18
Cumulative Var	0.27	0.49	0.67

Test of the hypothesis that 3 factors are sufficient.

The degrees of freedom for the model is 12 and the fit was 0.01  
The number of observations was 213 with Chi Square = 2.97 with  
prob < 1

# Factor analysis options

- I. factanal (MLE) is part of core R
- II. fa is part of psych
  - A. minres (ols) (default)
  - B. weighted least squares
  - C. generalized weighted least squares
  - D. maximum likelihood
  - E. principal axis

# Principal Components

```
> pc3
```

	V	PC1	PC2	PC3
Sentences	1	0.863		
Vocabulary	2	0.854	0.31	
Sent.Completion	3	0.849		
First.Letters	4		0.82	
4.Letter.Words	5		0.79	0.301
Suffixes	6	0.314	0.77	
Letter.Series	7			0.834
Pedigrees	8	0.534		0.613
Letter.Group	9		0.31	0.805

	PC1	PC2	PC3
SS loadings	2.73	2.25	1.99
Proportion Var	0.30	0.25	0.22
Cumulative Var	0.30	0.55	0.78

Test of the hypothesis that 3 factors are sufficient.

The degrees of freedom for the model is 12 and the fit was 0.62  
The number of observations was 213 with Chi Square = 127.9 with  
prob < 1.6e-21

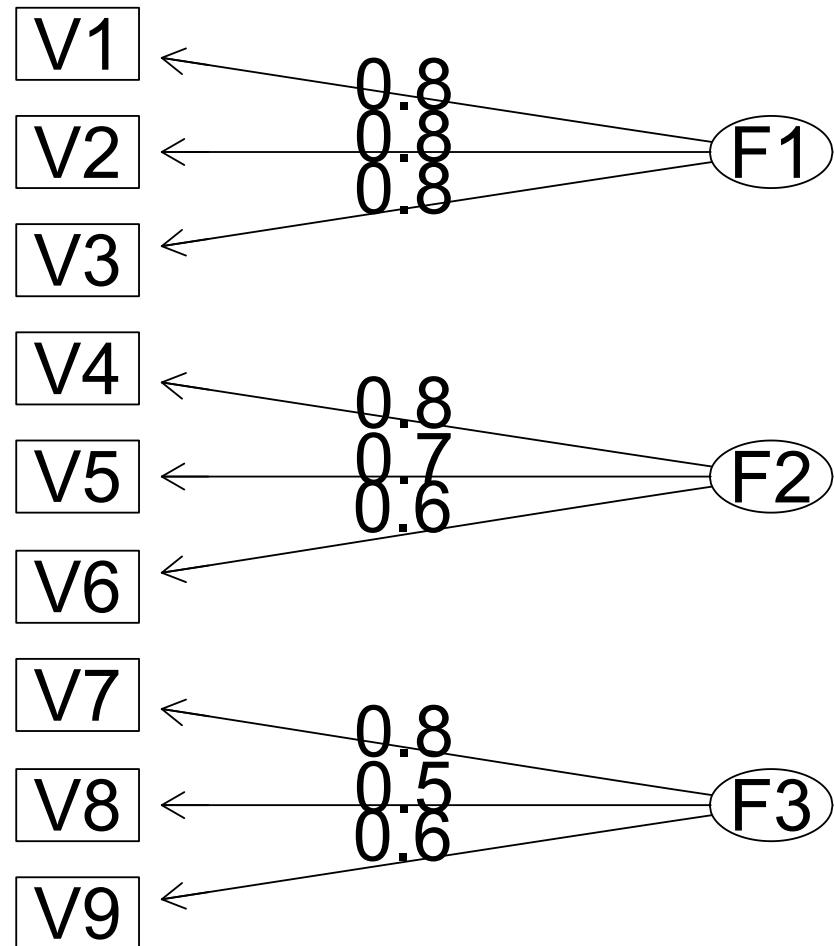
# Comparing solutions: factor congruence

```
> factor.congruence(list(f3,pa3,pc3))
```

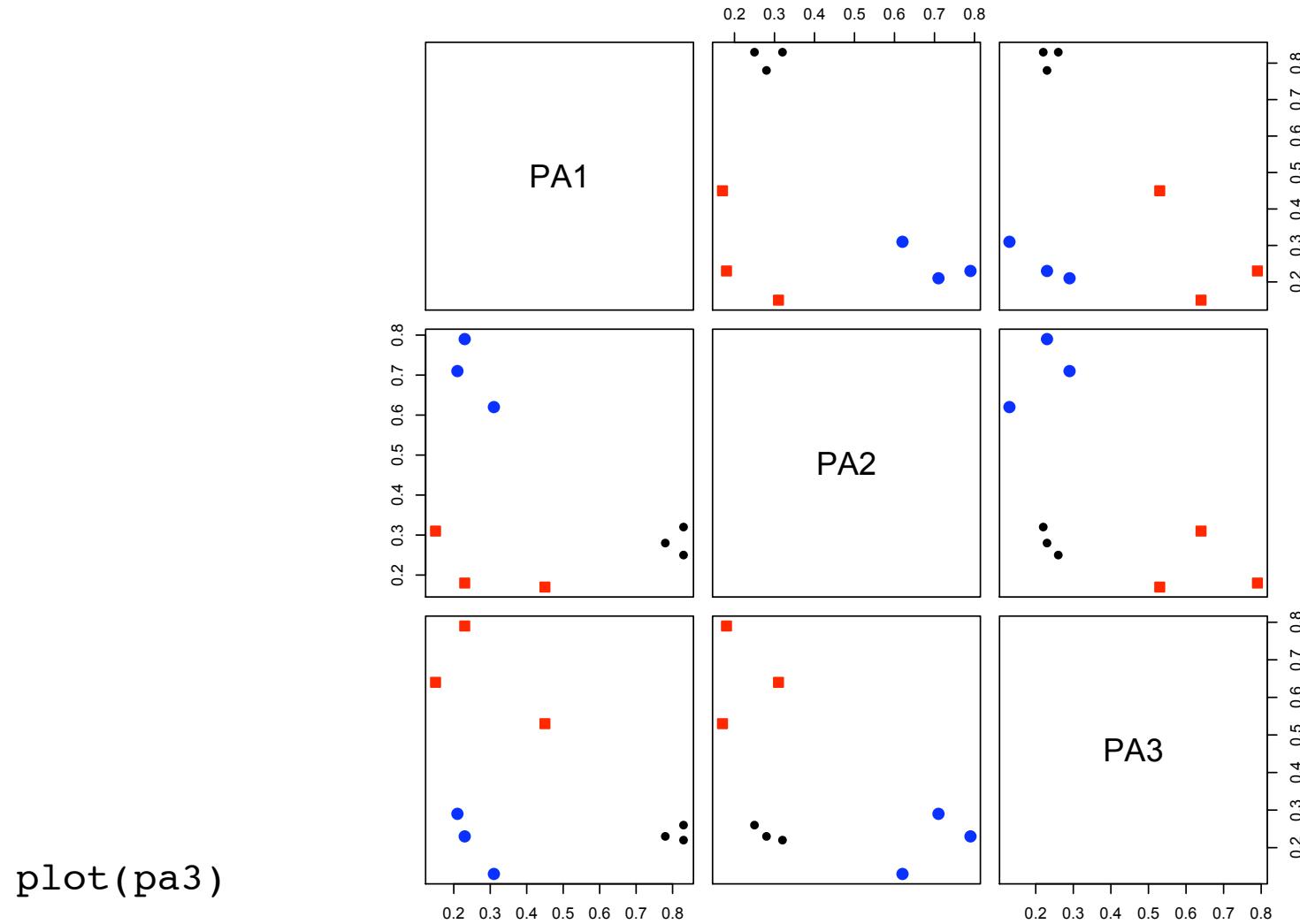
	Factor1	Factor2	Factor3	PA1	PA2	PA3	PC1	PC2	PC3
Factor1	1.00	0.64	0.62	1.00	0.64	0.62	1.00	0.59	0.55
Factor2	0.64	1.00	0.62	0.63	1.00	0.62	0.61	0.99	0.57
Factor3	0.62	0.62	1.00	0.62	0.62	1.00	0.61	0.56	0.99
PA1	1.00	0.63	0.62	1.00	0.64	0.62	1.00	0.59	0.55
PA2	0.64	1.00	0.62	0.64	1.00	0.62	0.61	0.99	0.57
PA3	0.62	0.62	1.00	0.62	0.62	1.00	0.61	0.56	0.99
PC1	1.00	0.61	0.61	1.00	0.61	0.61	1.00	0.56	0.54
PC2	0.59	0.99	0.56	0.59	0.99	0.56	0.56	1.00	0.50
PC3	0.55	0.57	0.99	0.55	0.57	0.99	0.54	0.50	1.00

# A misleading graph

Factor Analysis



# Plot the loadings: shows some cross loadings



# Rotations and transformations

I. Orthogonal rotations

A. Varimax, Quartimax

II. Oblique transformations

A. Promax, Oblimin, Quartimin,  
biquartimin, targeted, cluster, ...

```

> fa3o <- fa(Thurstone, 3, rotate = "oblimin")
Loading required package: GPArotation
> fa3o
Factor Analysis using method = minres
Call: fa(r = Thurstone, nfactors = 3, rotate = "oblimin")
    item   MR1   MR2   MR3   h2   u2
Sentences       1  0.90
Vocabulary      2  0.89
Sent.Completion 3  0.84
First.Letters    4          0.85
4.Letter.Words  5          0.75
Suffixes         6          0.63
Letter.Series    7          0.84  0.72  0.28
Pedigrees        8  0.38
Letter.Group     9          0.63  0.52  0.48
    MR1   MR2   MR3
SS loadings    2.64  1.87  1.49
Proportion Var 0.29  0.21  0.17
Cumulative Var 0.29  0.50  0.67
With factor correlations of
    MR1   MR2   MR3
MR1 1.00  0.59  0.53
MR2  0.59  1.00  0.52
MR3  0.53  0.52  1.00
Test of the hypothesis that 3 factors are sufficient.
The degrees of freedom for the model is 12 and the objective function

```

# Oblique solution Oblimin

```

> print(fa3o,cut=0)
Factor Analysis using method = minres
Call: fa(r = Thurstone, nfactors = 3, rotate = "oblimin")
      item   MR1    MR2    MR3    h2    u2
Sentences        1  0.90 -0.04  0.04  0.82  0.18
Vocabulary       2  0.89  0.06 -0.03  0.84  0.16
Sent.Completion   3  0.84  0.04  0.00  0.74  0.26
First.Letters     4  0.00  0.85  0.00  0.73  0.27
4.Letter.Words    5 -0.02  0.75  0.10  0.63  0.37
Suffixes          6  0.18  0.63 -0.08  0.50  0.50
Letter.Series     7  0.03 -0.01  0.84  0.72  0.28
Pedigrees         8  0.38 -0.05  0.47  0.50  0.50
Letter.Group      9 -0.06  0.21  0.63  0.52  0.48

```

	MR1	MR2	MR3
SS loadings	2.64	1.87	1.49
Proportion Var	0.29	0.21	0.17
Cumulative Var	0.29	0.50	0.67

With factor correlations of

	MR1	MR2	MR3
MR1	1.00	0.59	0.53
MR2	0.59	1.00	0.52
MR3	0.53	0.52	1.00

# Show all values!

```
> pa3p <- Promax(pa3)
> pa3p
```

	V	PA1	PA2	PA3
Sentences	1	0.911		
Vocab	2	0.904		
S.comp	3	0.848		
F.letter	4		0.869	
4.letter	5		0.759	
Suffix	6		0.650	
Series	7			0.8865
Pedi	8	0.350		0.4969
letters	9			0.6800

	PA1	PA2	PA3
SS loadings	2.54	1.80	1.52
Proportion Var	0.28	0.20	0.17
Cumulative Var	0.28	0.48	0.65

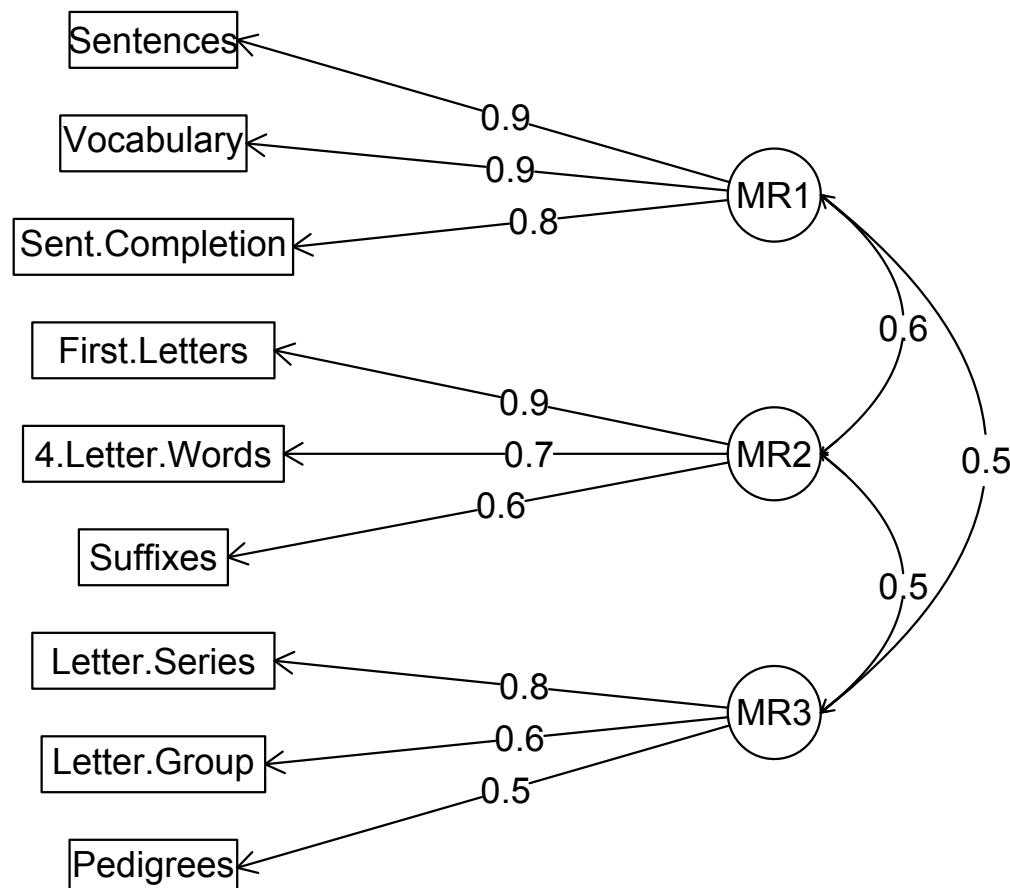
With factor correlations of

	PA1	PA2	PA3
PA1	1.00	0.61	0.61
PA2	0.61	1.00	0.58
PA3	0.61	0.58	1.00

# Oblique: Promax

# A more accurate graphic

3 oblique factors from Thurstone

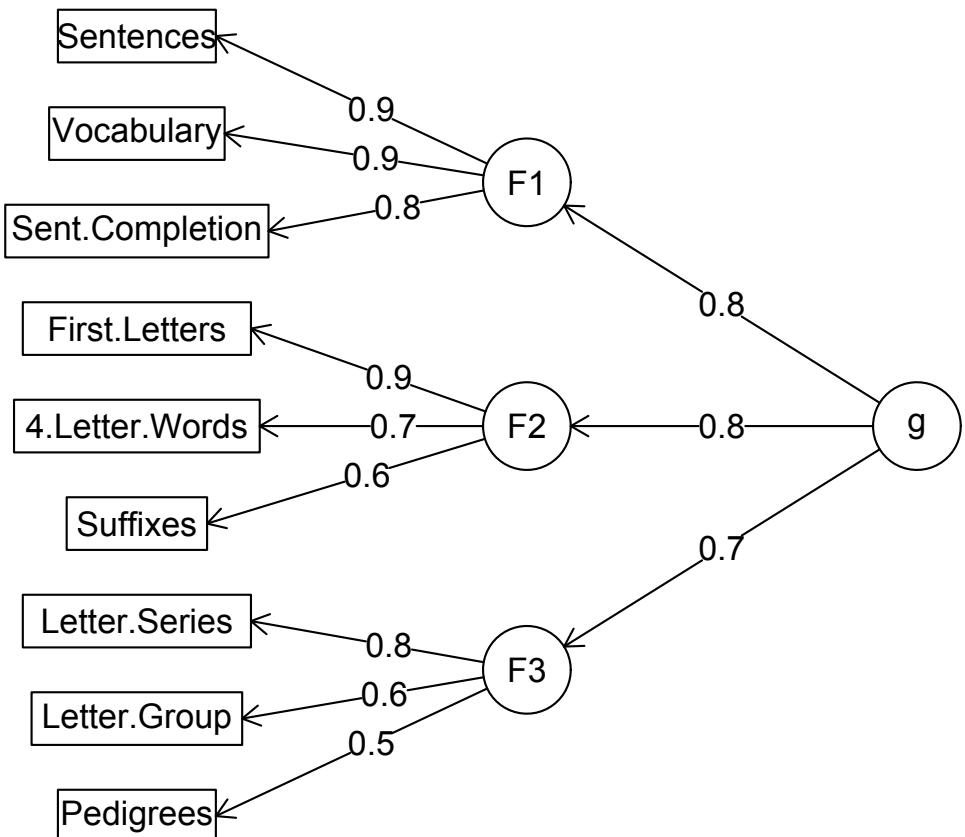
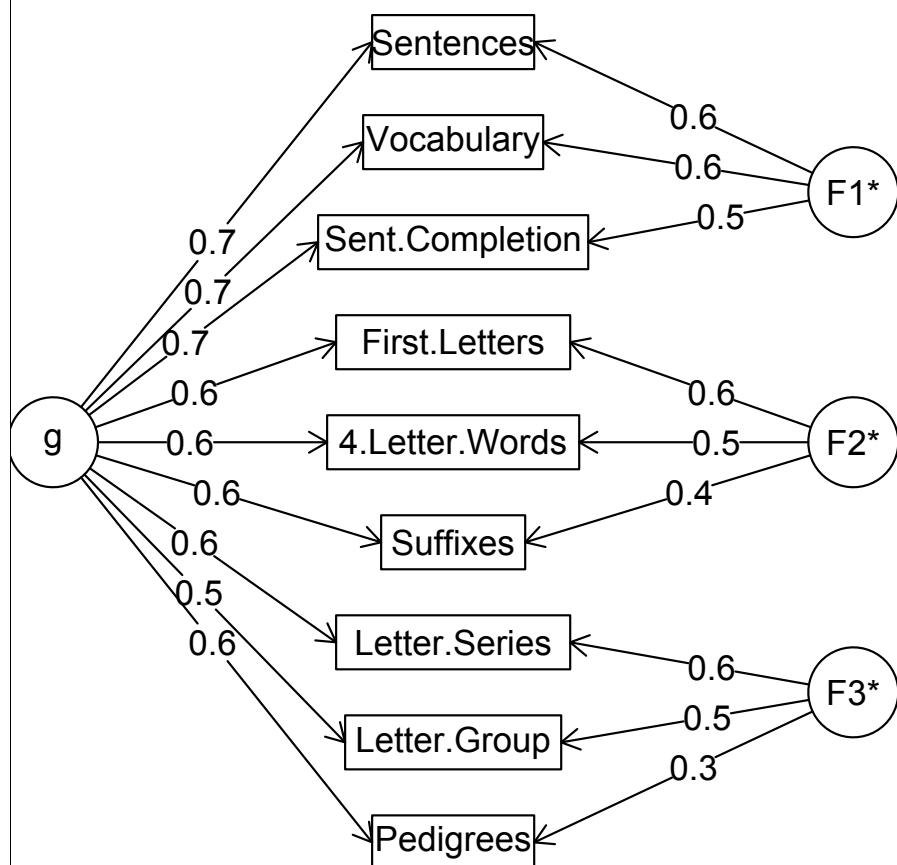


fa.diagram(fa3o)

nega with Schmid Leiman Transformation

Hierarchical (multilevel) Structure

# Hierarchical solutions



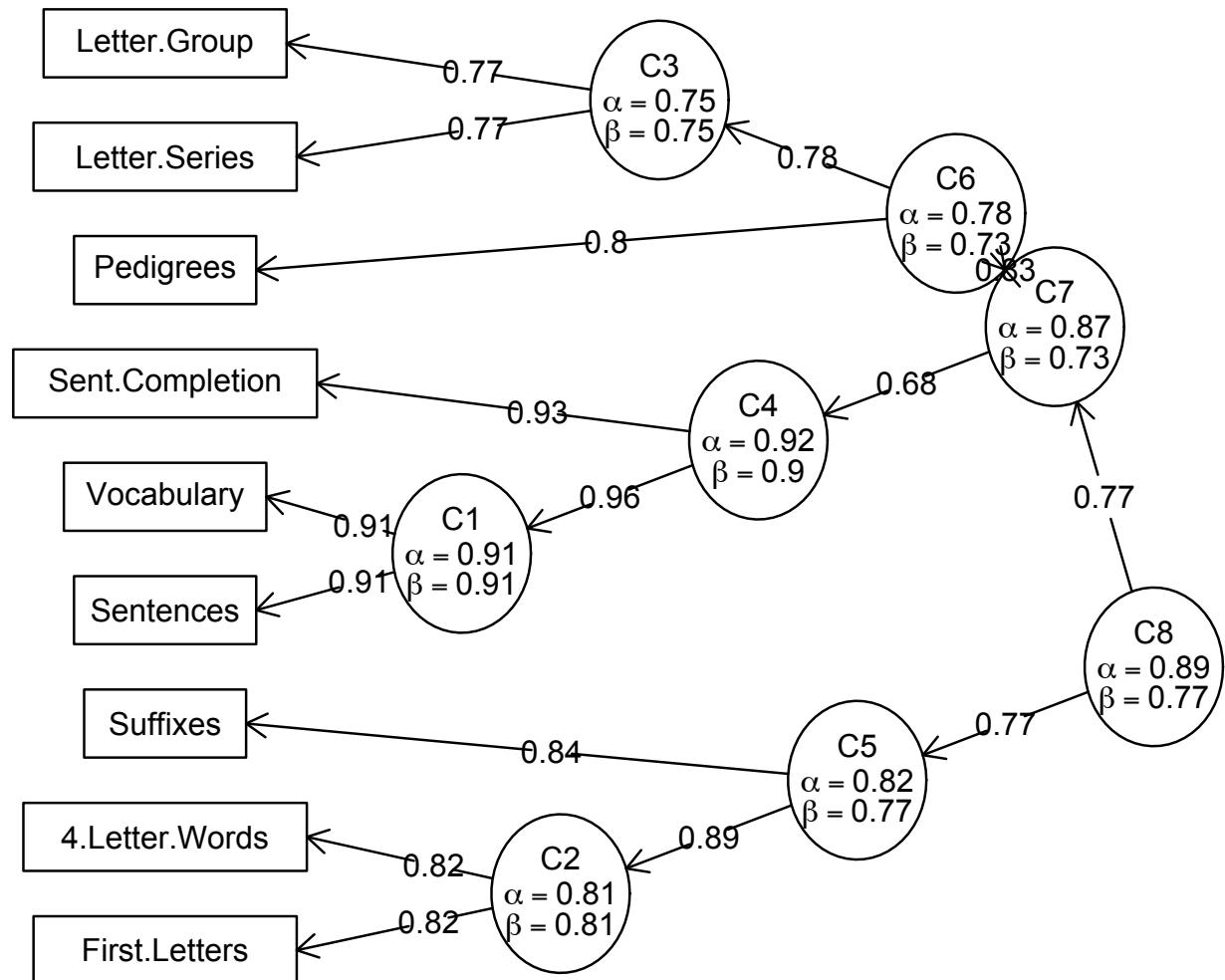
```
> omsl <-omega(Thurstone,title="Bifactor")
> omsl <-omega(Thurstone,sl=FALSE,title="Hierarchical")
```

# Hierarchical Clustering

- I. Find the similarity matrix (correlations)
- II. Find the most similar pair of items/tests
- III. Combine them and repeat II and III until some criterion (alpha, beta) fails to increase

# Hierarchical cluster analysis

ICLUST of Thurstone's 9 variables



# Multidimensional scaling

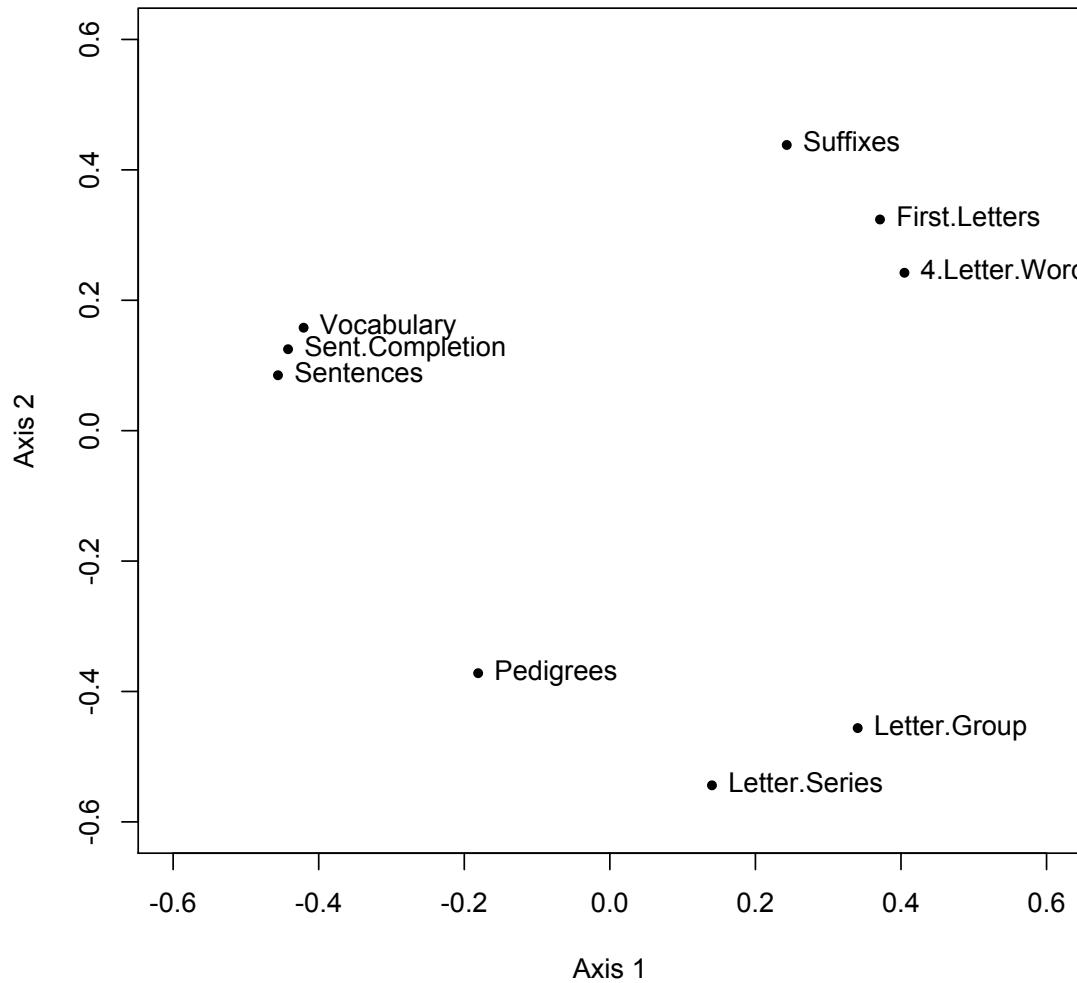
- I. Convert correlations to distances
- II. Multidimensional scaling will remove a general factor since it considers relative ranking of distances

# MDS

```
> Thurs.dist <- sqrt(2*(1-Thurstone))  
> mdsT <- cmdscale(Thurs.dist,2)  
> round(mdsT,2)
```

	[ ,1 ]	[ ,2 ]
Sentences	-0.46	0.08
Vocabulary	-0.42	0.16
Sent.Completion	-0.44	0.12
First.Letters	0.37	0.32
4.Letter.Words	0.40	0.24
Suffixes	0.24	0.44
Letter.Series	0.14	-0.54
Pedigrees	-0.18	-0.37
Letter.Group	0.34	-0.46

# MDS plot



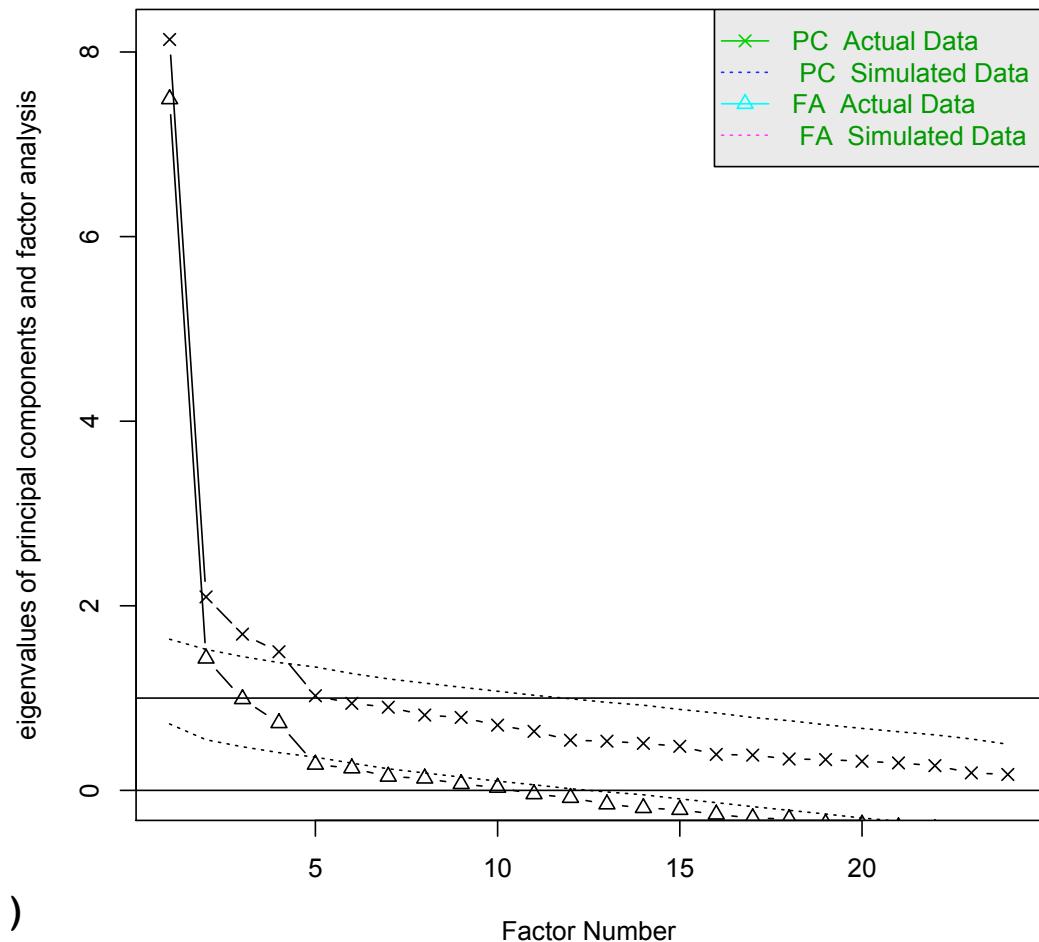
```
position <- rep(4,9)
plot(mdst,xlim=c(-.6,.6),ylim=c(-.6,.6),ylab="Axis 2",xlab="Axis 1")
text(mdst,rownames(mdst),pos=position)
```

# A more complex example

- I. Holzinger-Harman 24 mental ability tests
- II. Compare FA, CA, MDS

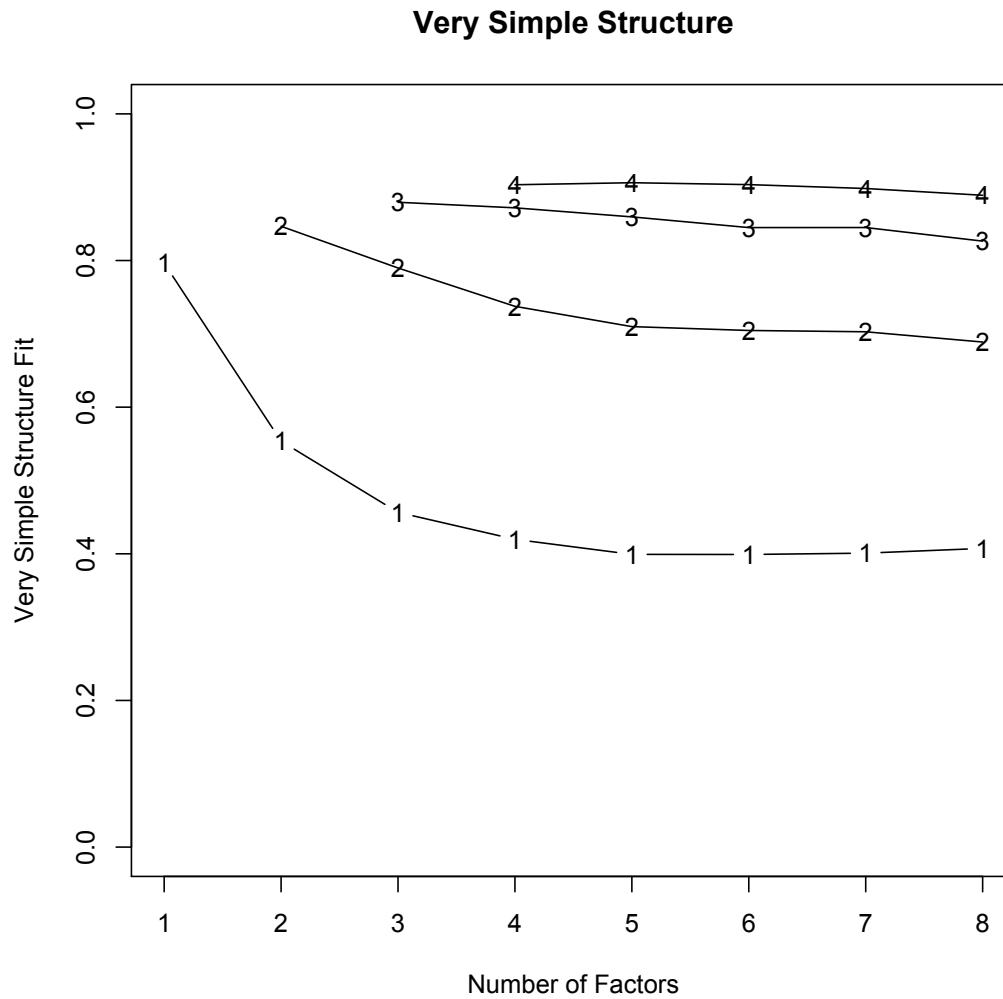
# Parallel analysis

Parallel Analysis Scree Plots



```
> hh <- Harman74.cor$cov  
> fa.parallel(hh,n.obs=228)
```

# VSS says 1 big factor



```
> vss <- VSS(hh, n.obs=228)
```

```
> vss
```

# MAP suggests 4

Very Simple Structure

Call: VSS(x = hh, n.obs = 228)

VSS complexity 1 achieves a maximum of 0.8 with 1 factors

VSS complexity 2 achieves a maximum of 0.85 with 2 factors

The Velicer MAP criterion achieves a minimum of 0.03 with 4 factors

Velicer MAP

```
[1] 0.02 0.02 0.02 0.02 0.02 0.02 0.03 0.03
```

Very Simple Structure Complexity 1

```
[1] 0.80 0.55 0.46 0.42 0.40 0.40 0.40 0.41
```

Very Simple Structure Complexity 2

```
[1] 0.00 0.85 0.79 0.74 0.71 0.70 0.70 0.69
```

# Chi square says > 8

```
> vss$vss.stats[,1:3]
  dof      chisq      prob
1 252 1012.9000 9.259262e-92
2 229  693.9911 2.649458e-48
3 207  485.1213 2.232607e-24
4 186  370.8825 2.174718e-14
5 166  307.7273 1.479600e-10
6 147  266.8324 5.628353e-09
7 129  226.6602 2.396296e-07
8 112  182.6407 2.832707e-05
>
```

```

<- fa4o <- factor.pain(4, n.obs=220, rotate= "oblique", 
> fa4o

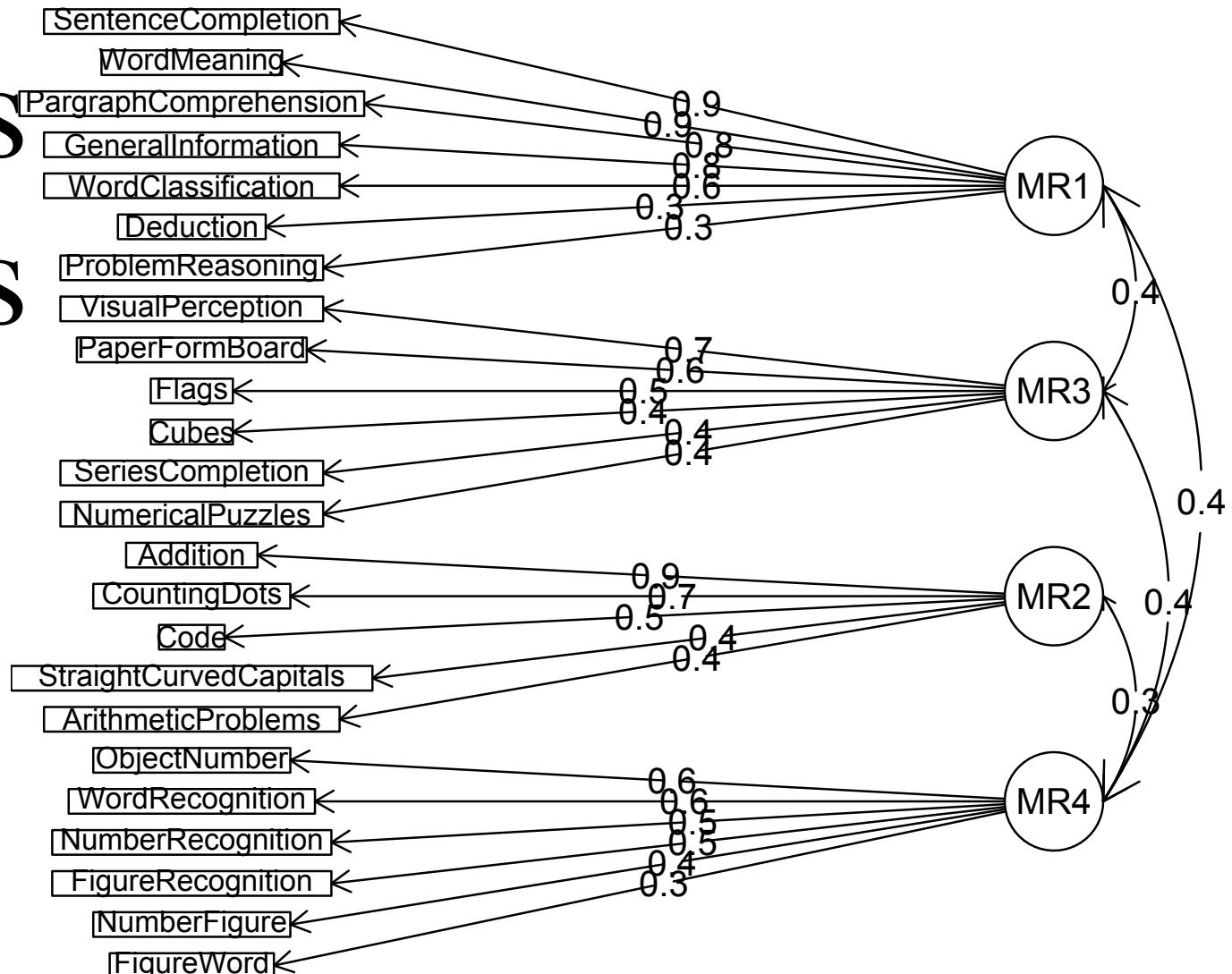
```

	V	PA1	PA3	PA2	PA4
VisualPerception	1		0.69		
Cubes	2		0.46		
PaperFormBoard	3		0.54		
Flags	4		0.52		
GeneralInformation	5	0.76			
ParagraphComprehension	6	0.80			
SentenceCompletion	7	0.87			
WordClassification	8	0.56			
WordMeaning	9	0.86			
Addition	10			0.86	
Code	11			0.49	0.30
CountingDots	12			0.70	
StraightCurvedCapitals	13		0.42	0.47	
WordRecognition	14				0.58
NumberRecognition	15				0.55
FigureRecognition	16		0.33		0.52
ObjectNumber	17				0.59
NumberFigure	18				0.43
FigureWord	19				0.32
Deduction	20	0.33	0.31		With factor correlations
NumericalPuzzles	21		0.37	0.33	PA1 PA3 PA2 PA4
ProblemReasoning	22	0.31	0.30		PA1 1.00 0.41 0.30 0.40
SeriesCompletion	23	0.30	0.44		PA3 0.41 1.00 0.27 0.38
ArithmeticProblems	24			0.41	PA2 0.30 0.27 1.00 0.32

# 4 oblique factors

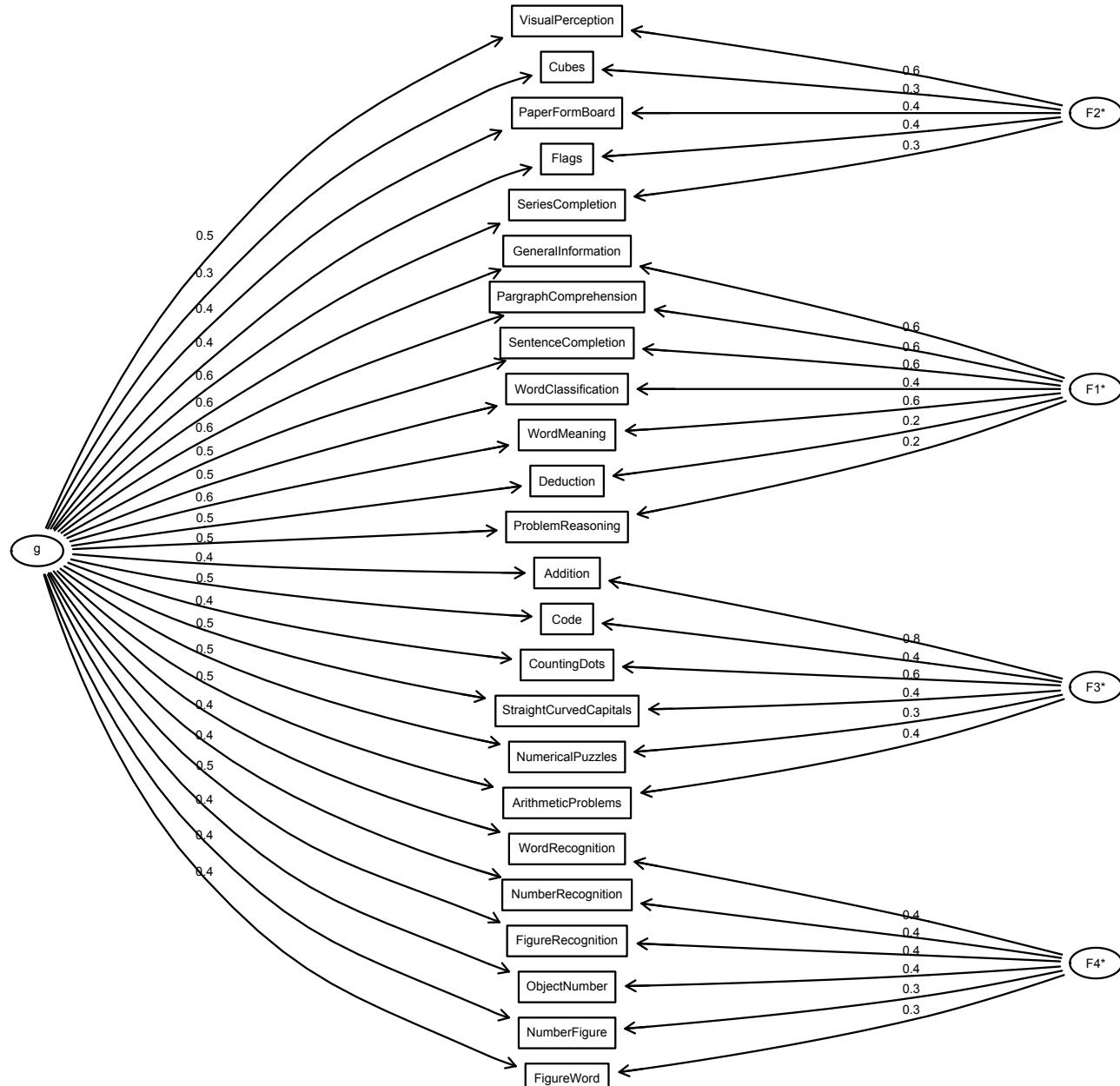
# 4 minres factors

## 4 oblique factors of the Holzinger-Harman problem

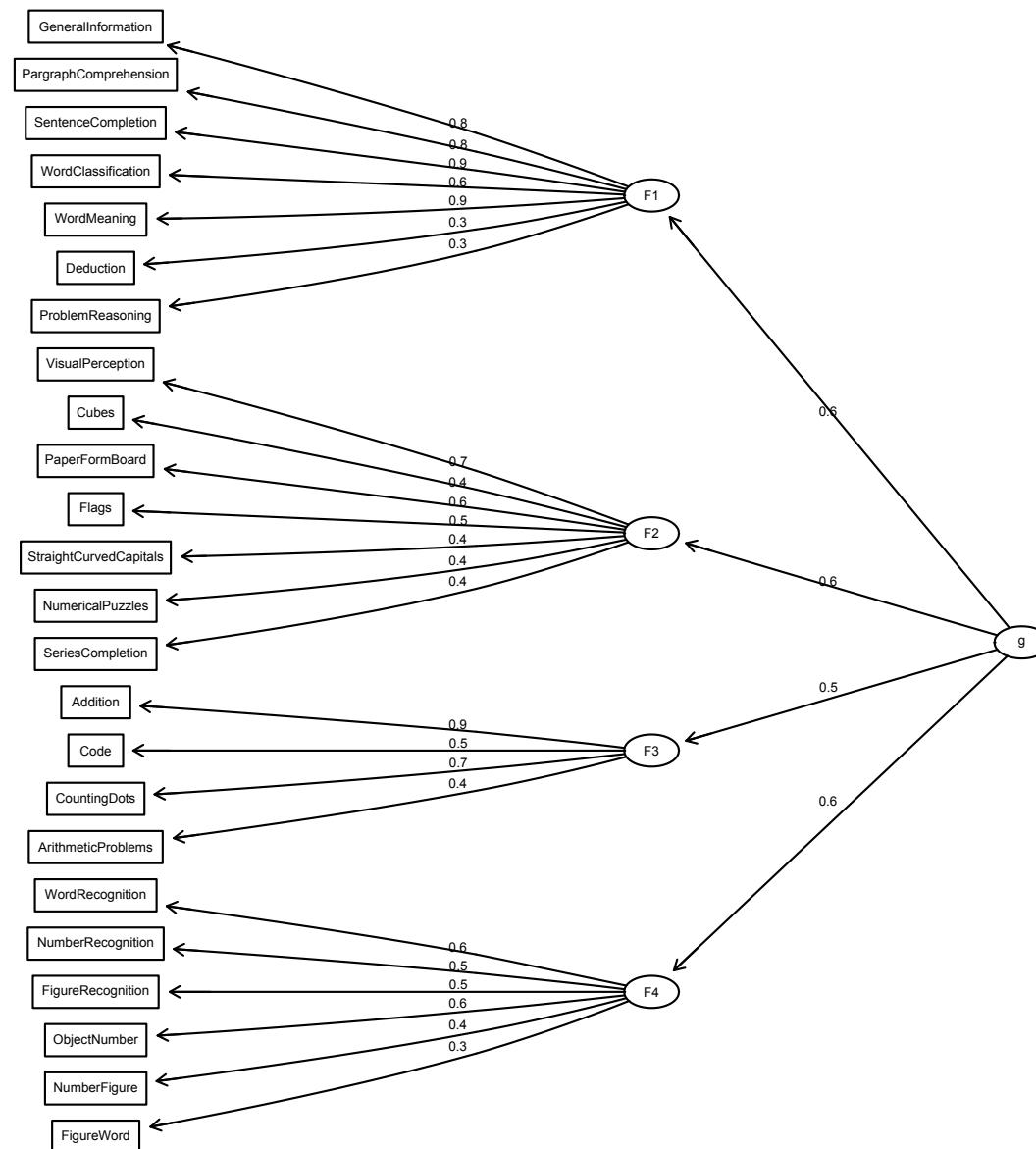


## Holzinger Harman problem -- Bifactor

```
om4 <-omega(hh,4,title="Holzinger Harman problem -- Bifactor")
```

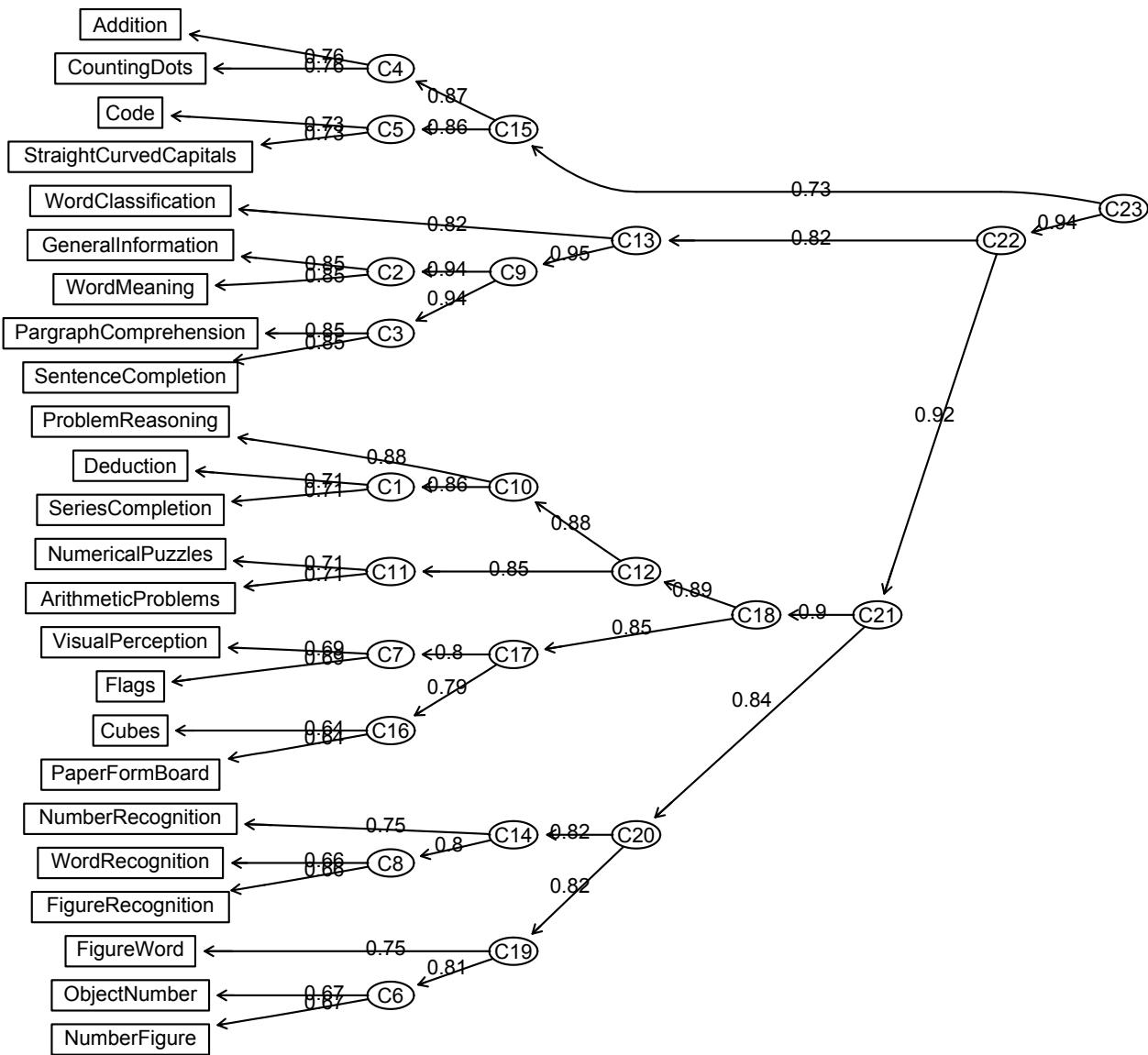


## Holzinger Harman problem -- Hierarchical



```
> om4 <-omega(hh,4,title="Holzinger Harman problem -- Hierarchical",sl=FALSE)
```

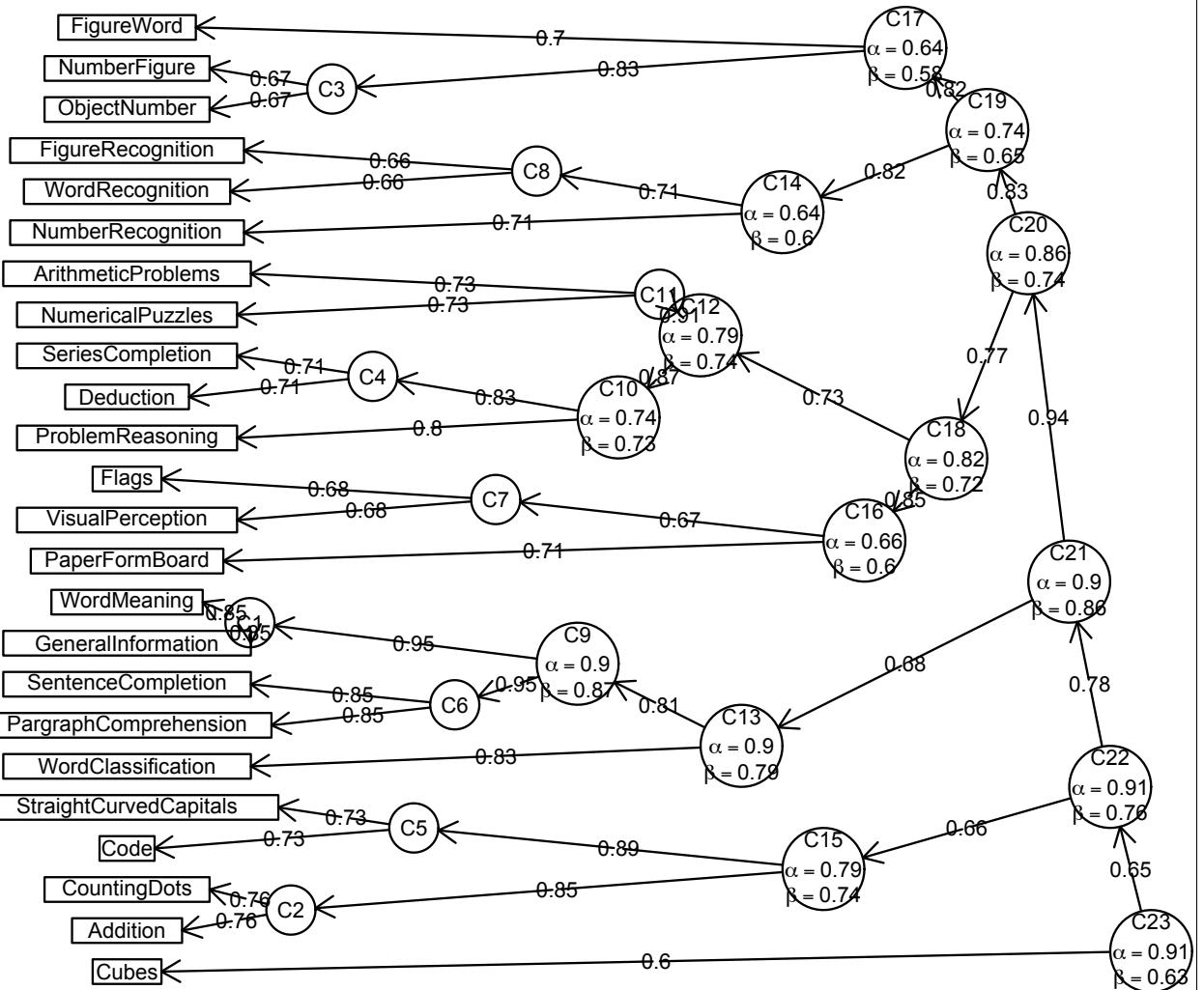
## ICLUST of Holzinger Harman 24 mental measurements



```
ic4 <- ICLUST(hh, title="ICLUST of Holzinger Harman 24 mental measurements")
```

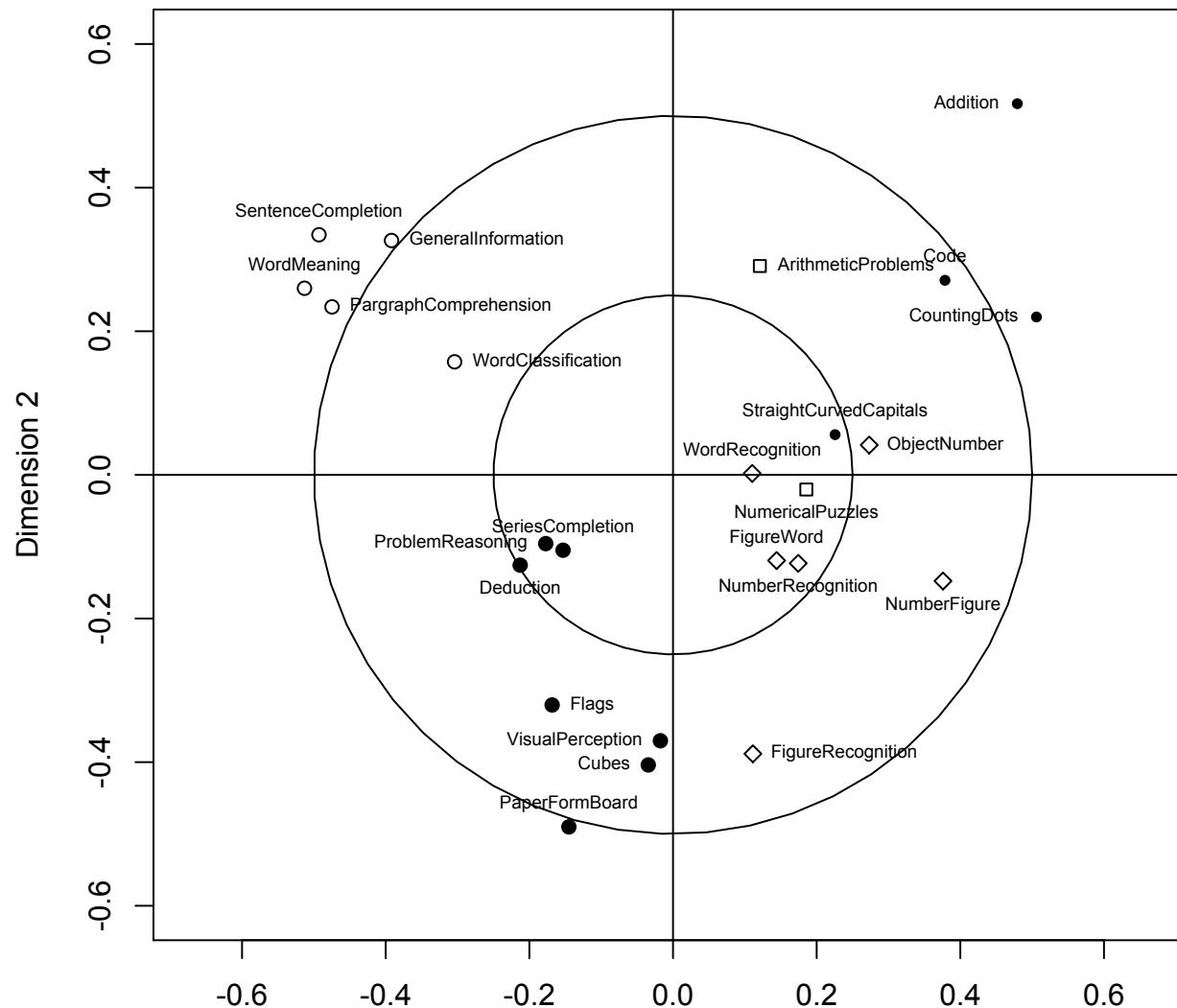
# Hierarchical cluster analysis

ICLUST of Holzinger-Harman problem



# MDS of HH problem

Multidimensional Scaling of 24 ability tests



# code for MDS plot

```
> dis24 <- sqrt(2*(1-Harman74.cor$cov))
> mds24 <- cmdscale(dis24,2)
> plot.char <- c( 19, 19, 19, 19,    21, 21,    21, 21,    21,
20, 20, 20,
+      20, 23, 23, 23,    23, 23, 23, 19,    22, 19, 19, 22 )
> plot(mds24,xlim=c(-.6,.6),ylim=c(-.6,.6),xlab="Dimension
1",ylab="Dimension 2",asp=1,pch=plot.char)
> position <- c(2,2,3,4,   4,4,3,4,   3,2,3,2,   3,3,1,4,
4,1,3,1,   1,2,3,4)
> text(mds24,rownames(mds24),cex=.6,pos=position)
> abline(v=0,h=0)
> title("Multidimensional Scaling of 24 ability tests")
> #draw circles at .25 and .50 units away from the center
> segments = 51
> angles <- (0:segments) * 2 * pi/segments
>           unit.circle <- cbind(cos(angles), sin(angles))
>           lines(unit.circle*.25)
>           lines(unit.circle*.5)
```

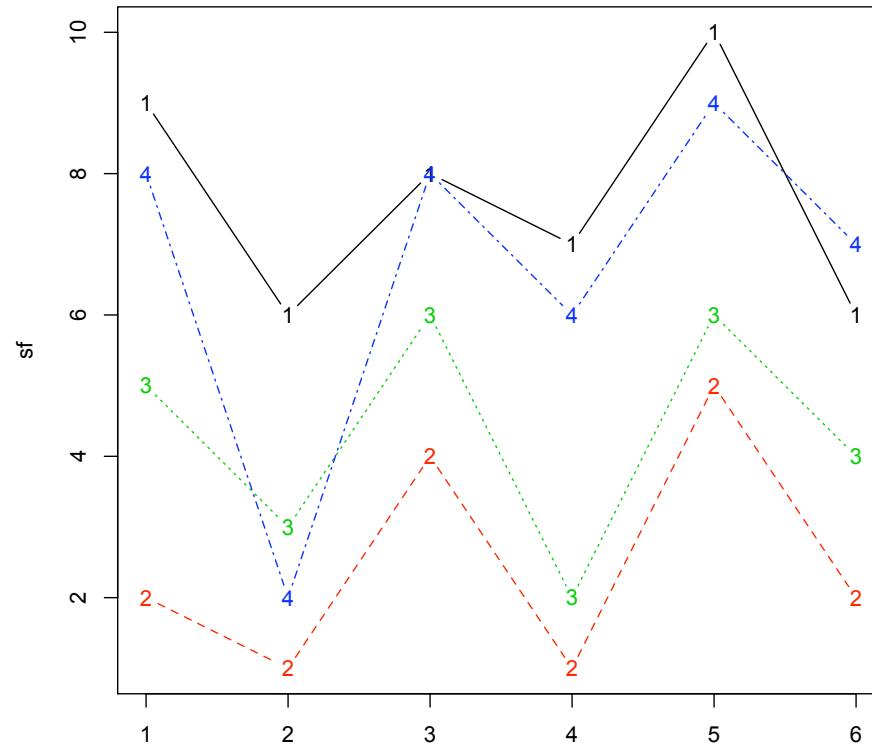
# Reliability of scales and raters

- I. First consider the reliability of raters using the IntraClass Correlation (see Shrout and Fleiss for the definitive discussion)
- II. Types of reliability of ratings (1 or n per target)
  - A. each target rated by a different judge, judges are random
  - B. random sample of k judges rate targets
  - C. Fixed set of k judges give ratings

# 4 judges rate 6 subjects

```
> sf
```

	J1	J2	J3	J4
S1	9	2	5	8
S2	6	1	3	2
S3	8	4	6	8
S4	7	1	2	6
S5	10	5	6	9
S6	6	2	4	7



# Simple correlations (these will remove means for raters)

```
> round(cor(sf),2)
      J1    J2    J3    J4
J1  1.00  0.75  0.73  0.75
J2  0.75  1.00  0.89  0.73
J3  0.73  0.89  1.00  0.72
J4  0.75  0.73  0.72  1.00
```

# ICC

```
> ICC(sf)
```

	type	ICC	F	df1	df2	p	lower bound	upper bound
Single_raters_absolute	ICC1	0.17	1.79	5	18	0.16	-0.13	0.72
Single_random_raters	ICC2	0.29	11.03	5	15	0.00	0.02	0.76
Single_fixed_raters	ICC3	0.71	11.03	5	15	0.00	0.34	0.95
Average_raters_absolute	ICC1k	0.44	1.79	5	18	0.16	-0.88	0.91
Average_random_raters	ICC2k	0.62	11.03	5	15	0.00	0.07	0.93
Average_fixed_raters	ICC3k	0.91	11.03	5	15	0.00	0.68	0.99

```
> alpha(sf)
```

## Alpha of raters

Reliability analysis

Call: alpha(x = sf)

raw_alpha	std.alpha	G6(smc)	average_r	mean	sd
0.91	0.93	0.92	0.76	21	6.7

Reliability if an item is dropped:

	raw_alpha	std.alpha	G6(smc)	average_r
J1	0.88	0.91	0.89	0.78
J2	0.87	0.89	0.85	0.73
J3	0.87	0.90	0.85	0.74
J4	0.92	0.92	0.90	0.79

## Item statistics

	n	r	r.cor	mean	sd
J1	6	0.89	0.83	7.7	1.6
J2	6	0.93	0.92	2.5	1.6
J3	6	0.92	0.91	4.3	1.6
J4	6	0.88	0.82	6.7	2.5

# Reliability of a single scale

```
> round(cor(bfi[,1:10],use="pairwise"),2)
```

	A1	A2	A3	A4	A5	C1	C2	C3	C4	C5
A1	1.00	-0.30	-0.23	-0.12	-0.19	-0.03	-0.06	0.01	0.19	0.08
A2	-0.30	1.00	0.39	0.24	0.41	0.06	0.06	0.22	-0.15	-0.12
A3	-0.23	0.39	1.00	0.27	0.45	0.07	0.12	0.16	-0.14	-0.12
A4	-0.12	0.24	0.27	1.00	0.22	0.07	0.17	0.08	-0.15	-0.17
A5	-0.19	0.41	0.45	0.22	1.00	0.10	0.06	0.20	-0.14	-0.10
C1	-0.03	0.06	0.07	0.07	0.10	1.00	0.44	0.41	-0.39	-0.23
C2	-0.06	0.06	0.12	0.17	0.06	0.44	1.00	0.35	-0.36	-0.24
C3	0.01	0.22	0.16	0.08	0.20	0.41	0.35	1.00	-0.37	-0.36
C4	0.19	-0.15	-0.14	-0.15	-0.14	-0.39	-0.36	-0.37	1.00	0.53
C5	0.08	-0.12	-0.12	-0.17	-0.10	-0.23	-0.24	-0.36	0.53	1.00

# Mindless reliability

```
> alpha(bfi[1:10])
```

Reliability analysis

```
Call: alpha(x = bfi[1:10])
```

raw_alpha	std.alpha	G6(smc)	average_r	mean	sd
0.19	0.25	0.44	0.032	40	4.7

Reliability if an item is dropped:

Item statistics

	raw_alpha	std.alpha	G6(smc)	average_r	n	r	r.cor	mean	sd	
A1	0.290	0.354	0.51	0.057	A1	1000	0.099	-0.21	2.3	1.3
A2	0.082	0.133	0.35	0.017	A2	994	0.508	0.47	4.8	1.1
A3	0.045	0.101	0.33	0.012	A3	989	0.552	0.54	4.6	1.2
A4	0.108	0.173	0.40	0.023	A4	993	0.448	0.31	4.8	1.4
A5	0.042	0.093	0.32	0.011	A5	988	0.563	0.55	4.6	1.2
C1	0.133	0.190	0.38	0.025	C1	997	0.421	0.34	4.4	1.2
C2	0.123	0.182	0.38	0.024	C2	997	0.434	0.35	4.2	1.3
C3	0.105	0.154	0.36	0.020	C3	995	0.478	0.44	4.3	1.3
C4	0.336	0.392	0.50	0.067	C4	986	0.005	-0.24	2.6	1.4
C5	0.329	0.364	0.49	0.060	C5	997	0.077	-0.17	3.5	1.5

# somewhat better reliability

```
> keys <- make.keys(10, list(all=c(-1, 2:8, -9, -10)))
> alpha(bfi[1:10], keys)
```

```
Reliability analysis
Call: alpha(x = bfi[1:10], keys = keys)
```

raw_alpha	std.alpha	G6(smc)	average_r	mean	sd
0.72	0.72	0.75	0.21	40	4.7

Reliability if an item is dropped:

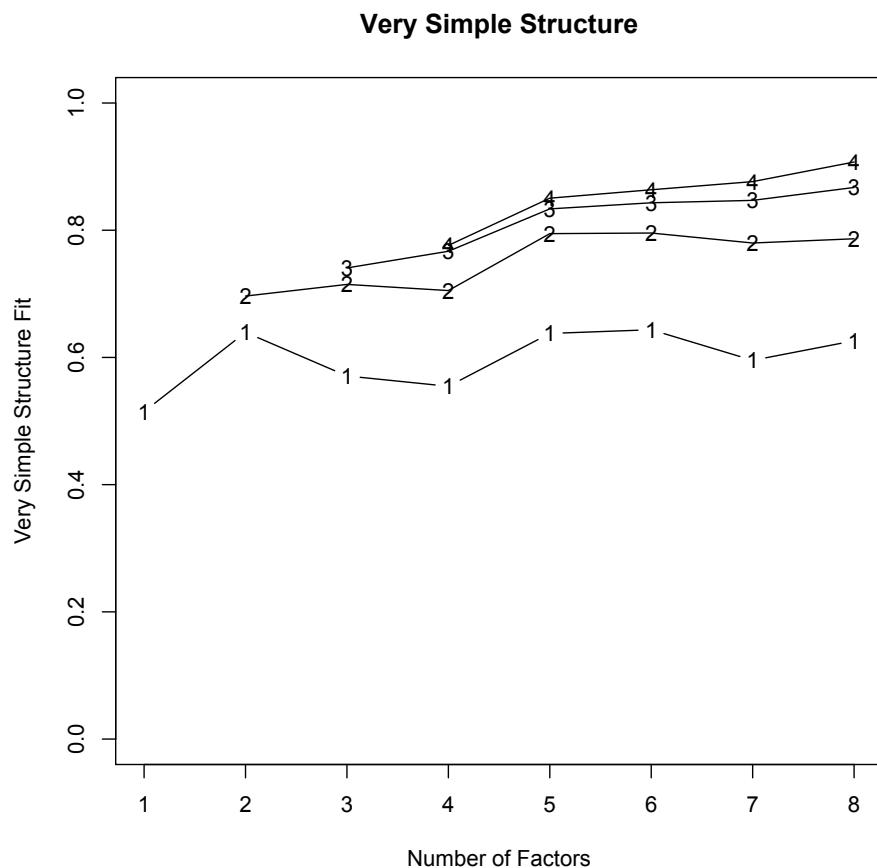
	raw_alpha	std.alpha	G6(smc)	average_r		n	r	r.cor	mean	sd
A1	0.72	0.72	0.74	0.23	A1	1000	0.41	0.29	2.3	1.3
A2	0.70	0.70	0.72	0.20	A2	994	0.55	0.49	4.8	1.1
A3	0.70	0.70	0.72	0.20	A3	989	0.55	0.49	4.6	1.2
A4	0.71	0.71	0.74	0.22	A4	993	0.46	0.35	4.8	1.4
A5	0.70	0.70	0.72	0.21	A5	988	0.53	0.46	4.6	1.2
C1	0.70	0.70	0.72	0.21	C1	997	0.52	0.46	4.4	1.2
C2	0.70	0.70	0.72	0.21	C2	997	0.54	0.47	4.2	1.3
C3	0.69	0.69	0.71	0.20	C3	995	0.59	0.54	4.3	1.3
C4	0.67	0.68	0.70	0.19	C4	986	0.64	0.61	2.6	1.4
C5	0.70	0.70	0.72	0.20	C5	997	0.55	0.49	3.5	1.5

# Examine the items

VSS suggests 2 factors!

## The items

- A1 Am indifferent to the feelings of others.
- A2 Inquire about others' well-being.
- A3 Know how to comfort others.
- A4 Love children.
- A5 Make people feel at ease.
- C1 Am exacting in my work.
- C2 Continue until everything is perfect.
- C3 Do things according to a plan.
- C4 Do things in a half-way manner.
- C5 Waste my time.



# Omega reliability

```
> om2 <- omega(bfi[1:10],2)
Warning messages:
1: In schmid(m, nfactors, pc, digits, rotate = rotate, n.obs =
n.obs, :
  Three factors are required for identification -- general factor
  loadings set to be equal. Proceed with caution.
2: In schmid(m, nfactors, pc, digits = digits, n.obs = n.obs, ...):
  Three factors are required for identification -- general factor
  loadings set to be equal. Proceed with caution.
```

```
> om2
Omega
Call: omega(m = bfi[1:10], nfactors = 2)
Alpha: 0.72
G.6: 0.75
Omega Hierarchical: 0.36
Omega Total 0.77
```

Schmid Leiman Factor loadings greater than 0.2

	g	F1*	F2*	h2	u2
A1-	0.21		0.30		0.87
A2	0.36		0.53	0.41	0.59
A3	0.36		0.55	0.43	0.57
A4	0.24		0.28		0.86
A5	0.36		0.54	0.42	0.58
C1	0.30	0.51		0.36	0.64
C2	0.30	0.48		0.32	0.68
C3	0.37	0.48		0.37	0.63
C4-	0.40	0.58		0.50	0.50
C5-	0.33	0.48		0.33	0.67

With eigenvalues of:

```
g F1* F2*
1.1 1.3 1.1
```

Omega h is  
low

```
> keys <- make.keys(10, list(all=c(-1,2:8,-9,-10), agree=c(-1,2:5), con=c(6:8,-9,-10)))
> score.items(keys, bfi[1:10])
Call: score.items(keys = keys, items = bfi[1:10])
```

(Unstandardized) Alpha:

	all	agree	con
alpha	0.72	0.65	0.74

Average item correlation:

	all	agree	con
average.r	0.2	0.27	0.36

Guttman 6\* reliability:

	all	agree	con
Lambda.6	0.74	0.62	0.72

Scale intercorrelations corrected for attenuation

raw correlations below the diagonal, alpha on the diagonal

corrected correlations above the diagonal:

	all	agree	con
all	0.72	1.10	1.13
agree	0.75	0.65	0.36
con	0.83	0.25	0.74

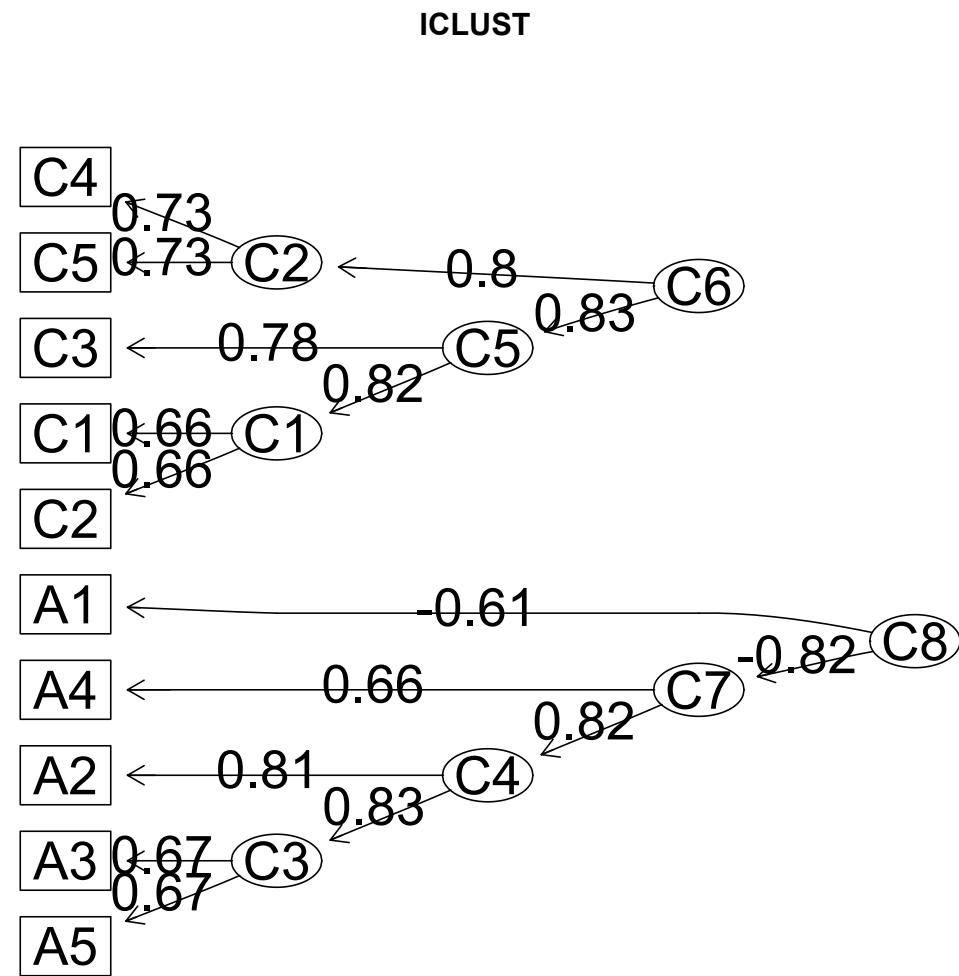
# Score 3 scales

# Item scale correlations

Item by scale correlations:  
corrected for item overlap and scale reliability

	all	agree	con
A1	-0.28	-0.37	-0.12
A2	0.47	0.63	0.21
A3	0.47	0.63	0.21
A4	0.34	0.37	0.22
A5	0.44	0.58	0.20
C1	0.46	0.13	0.59
C2	0.47	0.19	0.55
C3	0.54	0.25	0.60
C4	-0.62	-0.30	-0.69
C5	-0.50	-0.23	-0.56
>			

# ICLUST shows 2 scales



# Structural Equation modeling in R

- I. sem by John Fox
- II. does not do multiple group analyses
- III.Mx in R is a coming attraction
- IV.Using psych as a front end to sem to generate the model commands

# Using psych as front end to sem

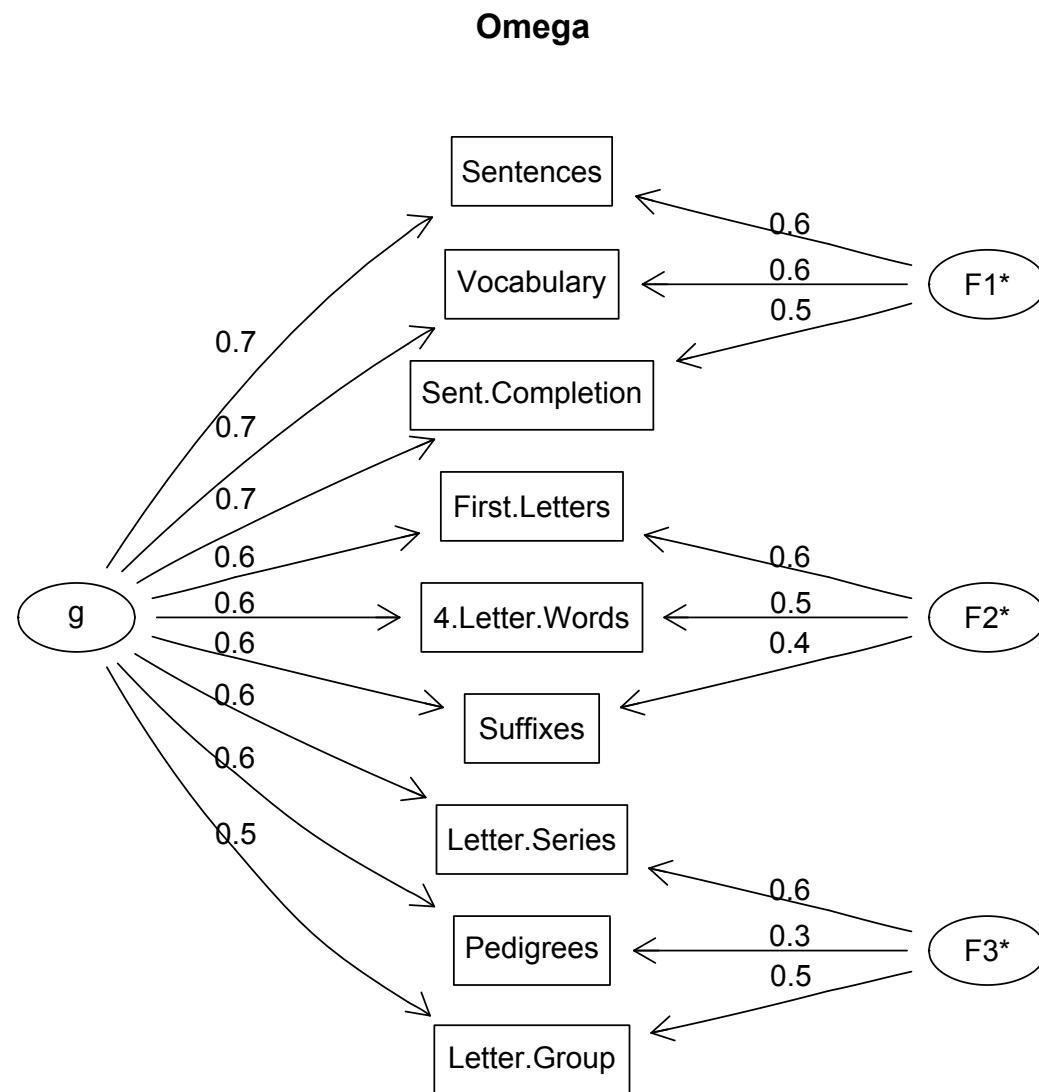
- I. Do the exploratory analysis (fa or omega) in psych
- II. output includes the sem model instructions
- III. run sem
- IV. (see the vignette on using psych for sem)

```
> om <- omega(Thurstone) #creates the path model and the model commands
> om$model
```

Path	Parameter	Initial
Value		
[1,] "g->Sentences"	"Sentences"	NA
[2,] "g->Vocabulary"	"Vocabulary"	NA
[3,] "g->Sent.Completion"	"Sent.Completion"	NA
[4,] "g->First.Letters"	"First.Letters"	NA
[5,] "g->4.Letter.Words"	"4.Letter.Words"	NA
[6,] "g->Suffixes"	"Suffixes"	NA
[7,] "g->Letter.Series"	"Letter.Series"	NA
[8,] "g->Pedigrees"	"Pedigrees"	NA
[9,] "g->Letter.Group"	"Letter.Group"	NA
[10,] "F1*->Sentences"	"F1*Sentences"	NA
[11,] "F1*->Vocabulary"	"F1*Vocabulary"	NA
[12,] "F1*->Sent.Completion"	"F1*Sent.Completion"	NA
[13,] "F2*->First.Letters"	"F2*First.Letters"	NA
[14,] "F2*->4.Letter.Words"	"F2*4.Letter.Words"	NA
[15,] "F2*->Suffixes"	"F2*Suffixes"	NA
[16,] "F3*->Letter.Series"	"F3*Letter.Series"	NA
[17,] "F3*->Pedigrees"	"F3*Pedigrees"	NA
[18,] "F3*->Letter.Group"	"F3*Letter.Group"	NA
[19,] "Sentences<->Sentences"	"e1"	NA
[20,] "Vocabulary<->Vocabulary"	"e2"	NA
[21,] "Sent.Completion<->Sent.Completion"	"e3"	NA
[22,] "First.Letters<->First.Letters"	"e4"	NA
[23,] "4.Letter.Words<->4.Letter.Words"	"e5"	NA
[24,] "Suffixes<->Suffixes"	"e6"	NA
[25,] "Letter.Series<->Letter.Series"	"e7"	NA
[26,] "Pedigrees<->Pedigrees"	"e8"	NA
[27,] "Letter.Group<->Letter.Group"	"e9"	NA

The  
model

# The model



# Do the sem

```
> library(sem)
> sem.bf <- sem(om$model,Thurstone,213)
> summary(sem.bf,digits=2)

Model Chisquare = 24    Df = 18 Pr(>Chisq) = 0.15
Chisquare (null model) = 1102    Df = 36
Goodness-of-fit index = 0.98
Adjusted goodness-of-fit index = 0.94
RMSEA index = 0.04    90% CI: (NA, 0.078)
Bentler-Bonnett NFI = 0.98
Tucker-Lewis NNFI = 0.99
Bentler CFI = 1
SRMR = 0.035
BIC = -72

Normalized Residuals
      Min.   1st Qu.   Median     Mean   3rd Qu.   Max.
-8.2e-01 -3.3e-01 -8.9e-07  2.8e-02  1.6e-01  1.8e+00
```

# Parameter values

Parameter Estimates

	Estimate	Std Error	z value	Pr(> z )	
Sentences	0.77	0.073	10.57	0.0e+00	Sentences <--- g
Vocabulary	0.79	0.072	10.92	0.0e+00	Vocabulary <--- g
Sent.Completion	0.75	0.073	10.27	0.0e+00	Sent.Completion <--- g
First.Letters	0.61	0.072	8.43	0.0e+00	First.Letters <--- g
4.Letter.Words	0.60	0.074	8.09	6.7e-16	4.Letter.Words <--- g
Suffixes	0.57	0.071	8.00	1.3e-15	Suffixes <--- g
Letter.Series	0.57	0.074	7.63	2.3e-14	Letter.Series <--- g
Pedigrees	0.66	0.069	9.55	0.0e+00	Pedigrees <--- g
Letter.Group	0.53	0.079	6.71	2.0e-11	Letter.Group <--- g
F1*Sentences	0.49	0.085	5.71	1.1e-08	Sentences <--- F1*
F1*Vocabulary	0.45	0.090	5.00	5.7e-07	Vocabulary <--- F1*
F1*Sent.Completion	0.40	0.093	4.33	1.5e-05	Sent.Completion <--- F1*
F2*First.Letters	0.61	0.086	7.16	8.2e-13	First.Letters <--- F2*
F2*4.Letter.Words	0.51	0.085	5.96	2.5e-09	4.Letter.Words <--- F2*
F2*Suffixes	0.39	0.078	5.04	4.7e-07	Suffixes <--- F2*
F3*Letter.Series	0.73	0.159	4.56	5.1e-06	Letter.Series <--- F3*
F3*Pedigrees	0.25	0.089	2.77	5.6e-03	Pedigrees <--- F3*
F3*Letter.Group	0.41	0.122	3.35	8.1e-04	Letter.Group <--- F3*
e1	0.17	0.034	5.05	4.4e-07	Sentences <--> Sentences
e2	0.17	0.030	5.65	1.6e-08	Vocabulary <--> Vocabulary
e3	0.27	0.033	8.09	6.7e-16	Sent.Completion <--> Sent.Com
e4	0.25	0.079	3.18	1.5e-03	First.Letters <-First.Letters
e5	0.39	0.063	6.13	8.8e-10	4.Letter.Words <--> 4.Letter.W
e6	0.52	0.060	8.68	0.0e+00	Suffixes <--> Suffixes
e7	0.15	0.223	0.67	5.0e-01	Letter.Series <--> Letter.Ser
e8	0.50	0.060	8.39	0.0e+00	Pedigrees <--> Pedigrees

# Programming in R

I. Very high level language

- A.interpreted at run time
- B.can integrate Fortran or C++ code

II. 3 ways of developing code

- A.cut and paste from an editor
- B.Modify prior code by adding or changing a function
- C.source from a file
- D.build a package for local or global distribution

# Programming in R

## I. functions and data structures

- A. The output of all functions is an object that will have a certain structure
- B. Part of the structure might be invisible but can be shown with the str() command.
  1. f3 <- fa(Thurstone,3,rotate=oblimin)
  2. str(f3) #will show more than just asking for f3

# selected output

```
> f3 <- fa(Thurstone,3,rotate="oblimin")
> f3
Factor Analysis using method = minres
Call: fa(r = Thurstone, nfactors = 3, rotate = "oblimin")
      item   MR1   MR2   MR3   h2   u2
Sentences       1  0.90          0.82  0.18
Vocabulary      2  0.89          0.84  0.16
Sent.Completion 3  0.84          0.74  0.26
First.Letters    4           0.85  0.73  0.27
4.Letter.Words  5           0.75  0.63  0.37
Suffixes         6           0.63  0.50  0.50
Letter.Series    7           0.84  0.72  0.28
Pedigrees        8  0.38          0.47  0.50  0.50
Letter.Group     9           0.63  0.52  0.48
      MR1   MR2   MR3
SS loadings    2.64  1.87  1.49
Proportion Var 0.29  0.21  0.17
Cumulative Var 0.29  0.50  0.67
With factor correlations of
      MR1   MR2   MR3
MR1 1.00  0.59  0.53
MR2 0.59  1.00  0.52
MR3 0.53  0.52  1.00
Test of the hypothesis that 3 factors are sufficient.
The degrees of freedom for the model is 12 and the objective function was 0.01
Fit based upon off diagonal values = 1
Measures of factor score adequacy
      [,1] [,2] [,3]
Correlation of scores with factors 0.96  0.92  0.90
Multiple R square of scores with factors 0.93  0.85  0.82
Minimum correlation of factor score estimates 0.86  0.71  0.63
```

# All the output (too much)

```

> print(f3,all=TRUE)
Factor Analysis using method = minres
Call: fa(r = Thurstone, nfactors = 3, rotate = "oblimin")
      item   MR1    MR2    MR3   h2   u2
Sentences     1  0.90       0.82  0.18
Vocabulary    2  0.89       0.84  0.16
Sent.Completion 3  0.84       0.74  0.26
First.Letters  4       0.85       0.73  0.27
4.Letter.Words 5       0.75       0.63  0.37
Suffixes       6       0.63       0.50  0.50
Letter.Series  7       0.84       0.72  0.28
Pedigrees      8       0.38       0.47  0.50
Letter.Group   9       0.63       0.52  0.48

      MR1    MR2    MR3
SS loadings  2.64  1.87  1.49
Proportion Var 0.29  0.21  0.17
Cumulative Var 0.29  0.50  0.67

With factor correlations of
      MR1    MR2    MR3
MR1  1.00  0.59  0.53
MR2  0.59  1.00  0.52
MR3  0.53  0.52  1.00

Test of the hypothesis that 3 factors are sufficient.

The degrees of freedom for the model is 12 and the objective function was  0.01

Fit based upon off diagonal values = 1
Measures of factor score adequacy
      [,1]  [,2]  [,3]
Correlation of scores with factors 0.96  0.92  0.90
Multiple R square of scores with factors 0.93  0.85  0.82
Minimum correlation of factor score estimates 0.86  0.71  0.63
$residual
      Sentences Vocabulary Sent.Completion First.Letters 4.Letter.Words
Sentences  0.1797970835  0.003569352  0.001056412 -0.0053521359  0.0054931042
Vocabulary 0.0035693518  0.164376546 -0.004726931  0.0015287573 -0.0013163850
Sent.Completion 0.0010564117 -0.004726931  0.264475270  0.0064257822 -0.0061643080
First.Letters -0.0053521359  0.001528757  0.006425782  0.2708794227 -0.0007462237
4.Letter.Words 0.0054931042 -0.001316385 -0.006164308 -0.0007462237  0.3691635597
Suffixes      -0.0005413284  0.003307528 -0.006202623  0.0009046706 -0.0007702702
Letter.Series -0.0001193089  0.005601586 -0.009592364  0.0036158583 -0.0048190635
Pedigrees     -0.0103409056 -0.003359723  0.020557454 -0.0045780810  0.0019664267
Letter.Group   0.0074095333 -0.010637633  0.007277838 -0.0037248900  0.0083593427
      Suffixes Letter.Series Pedigrees Letter.Group
Sentences     -0.0005413284 -0.0001193089 -0.010340906  0.0074095333

$fit
[1] 0.9569096

$fit.off
[1] 0.9998501

$factors
[1] 3

$n.obs
[1] NA

$PVAL
[1] NA

$dof
[1] 12

$objective
[1] 0.01390055

$criteria
objective
0.01390055           NA           NA

$Call
fa(r = Thurstone, nfactors = 3, rotate = "oblimin")

$r.scores
      [,1]      [,2]      [,3]
[1,] 1.0000000 0.6615062 0.6122765
[2,] 0.6615062 1.0000000 0.6134362
[3,] 0.6122765 0.6134362 1.0000000

$R2
[1] 0.9285797 0.8525374 0.8161127

$valid
[1] 0.9598034 0.9078568 0.8823116

```

# Using str to show what is there

```
> f3 <- fa(Thurstone,3,rotate="oblimin")
> str(f3)
List of 22
 $ residual      : num [1:9, 1:9] 0.1798 0.00357 0.00106 -0.00535 0.00549 ...
  ..- attr(*, "dimnames")=List of 2
  ... ..$ : chr [1:9] "Sentences" "Vocabulary" "Sent.Completion" "First.Letters" ...
  ... ..$ : chr [1:9] "Sentences" "Vocabulary" "Sent.Completion" "First.Letters" ...
 $ fit           : num 0.957
 $ fit.off       : num 1
 $ factors       : num 3
 $ n.obs         : logi NA
 $ PVAL          : logi NA
 $ dof           : num 12
 $ objective     : num 0.0139
 $ criteria      : Named num [1:3] 0.0139 NA NA
  ..- attr(*, "names")= chr [1:3] "objective" "" ""
 $ Call          : language fa(r = Thurstone, nfactors = 3, rotate = "oblimin")
 $ r.scores      : num [1:3, 1:3] 1 0.662 0.612 0.662 1 ...
 $ R2            : num [1:3] 0.929 0.853 0.816
 $ valid          : num [1:3] 0.96 0.908 0.882
 $ score.cor     : num [1:3, 1:3] 1 0.571 0.574 0.571 1 ...
 $ weights        : num [1:9, 1:3] 0.35332 0.38596 0.2284 0.01086 0.00503 ...
  ..- attr(*, "dimnames")=List of 2
  ... ..$ : chr [1:9] "Sentences" "Vocabulary" "Sent.Completion" "First.Letters" ...
  ... ..$ : NULL
 $ communality   : Named num [1:9] 0.82 0.84 0.74 0.73 0.63 0.5 0.72 0.5 0.52
  ..- attr(*, "names")= chr [1:9] "Sentences" "Vocabulary" "Sent.Completion" "First.Letters" ...
 $ uniquenesses: Named num [1:9] 0.18 0.16 0.26 0.27 0.37 0.5 0.28 0.5 0.48
  ..- attr(*, "names")= chr [1:9] "Sentences" "Vocabulary" "Sent.Completion" "First.Letters" ...
 $ values         : num [1:9] 4.85 1.09 1.04 0.48 0.45 0.37 0.32 0.23 0.17
 $ loadings       : loadings [1:9, 1:3] 0.90356 0.889 0.83522 -0.00297 -0.01535 ...
  ..- attr(*, "dimnames")=List of 2
  ... ..$ : chr [1:9] "Sentences" "Vocabulary" "Sent.Completion" "First.Letters" ...
  ... ..$ : chr [1:3] "MR1" "MR2" "MR3"
 $ fm             : chr "minres"
 $ Phi            : num [1:3, 1:3] 1 0.592 0.535 0.592 1 ...
 $ fn             : chr "fa"
 - attr(*, "class")= chr [1:2] "psych" "fa"
```

# Programming in R

I. Data types

II. operators

III. simple functions

IV. Writing functions

# Data structures

- I. elements: logical, integer, real, character, factor
- II. vectors: ordered sets of elements of one type
- III. matrices: ordered sets of vectors (all of one type)
- IV. data.frames: ordered sets of vectors, may be different types
- V. lists: ordered set of anything

# Operators

## I. arithmetical

1.  $+, -, *, /, ^, \%, \%$

2.  $a + b, a - b, a * b, a / b, a ^ b, a \% b$

## II. Logical

A.  $a == b, !a, a != b, a > b, a < b, a >= b, a <= b$

## III. Matrix

A.  $\% * \%$  is matrix multiplication

B.  $\% o \%$  is outer product

```
> a <- 2
> b <- 3
> v <- 5:10
> w <- 6:7
> v
[1] 5 6 7 8 9 10
> w
[1] 6 7
> v ^a
[1] 25 36 49 64 81 100
> w* b
[1] 18 21
> w * v
[1] 30 42 42 56 54 70
```

# example operations

# Matrix operations

```
> v
[1] 5 6 7 8 9 10
> t(v)
[,1] [,2] [,3] [,4] [,5] [,6]
[1,] 5 6 7 8 9 10
> t(v) %*% v
[,1]
[1,] 355
> v %*% t(v)
[,1] [,2] [,3] [,4] [,5] [,6]
[1,] 25 30 35 40 45 50
[2,] 30 36 42 48 54 60
[3,] 35 42 49 56 63 70
[4,] 40 48 56 64 72 80
[5,] 45 54 63 72 81 90
[6,] 50 60 70 80 90 100
```

# Additional matrix operators

outer  
product

```
> v
[1] 5 6 7 8 9 10
> w
[1] 6 7
> v %o% w
     [,1] [,2]
[1,]   30   35
[2,]   36   42
[3,]   42   49
[4,]   48   56
[5,]   54   63
[6,]   60   70
```

matrix “addition”  
(psych)

```
> x <- seq(4,8,2)
> x
[1] 4 6 8
> x %+% t(x)
     [,1] [,2] [,3]
[1,]    8   10   12
[2,]   10   12   14
[3,]   12   14   16
```

kronecker

# Functions

- I. Operate on an object and provide a new object
- II. e.g., `f <- function(x) {x * 2}`

```
> f <- function(x) {x * 2}  
> f(43)  
[1] 86  
> x  
[1] 4 6 8  
> f(x)  
[1] 8 12 16  
> f(v %o% w)  
      [,1] [,2]  
[1,]    60   70  
[2,]    72   84  
[3,]    84   98  
[4,]    96  112  
[5,]   108  126  
[6,]   120  140
```

# Simple functions

# a subset of useful functions

- I. `is.na()`, `is.null()`, `is.vector()`, `is.matrix()`, `is.list()`
- II. `sum()`, `rowSums()`, `colSums()`, `mean(x)`,  
`rowMeans()`, `colMeans()`, `max`, `min`, `median`  
(these work on the entire matrix)
- III. `var`, `cov`, `cor`, `sd` (these work on the columns  
of the matrix/`data.frame`)
- IV. `help.start()` brings up a web page of manuals

# More useful functions

- I. `rep(x,n)` (repeats the value x n times)
- II. `c(x,y)` (combines x with y)
- III. `cbind(x,y)` combines column wise
- IV. `rbind(x,y)` combines rowwise
- V. `seq(a,b,c)` sequence from a to b stepping by c

# sums on matrices and data.frames

```
> z <- f( v %o% w)
> z
      [,1] [,2]
[1,]    60   70
[2,]    72   84
[3,]    84   98
[4,]    96  112
[5,]   108  126
[6,]   120  140

> rowSums(z)
[1] 130 156 182 208 234 260
> colSums(z)
[1] 540 630
> mean(z)
[1] 97.5
> rowMeans(z)
[1] 65 78 91 104 117 130
> median(z)
[1] 97
```

```
> var(z)
      [,1] [,2]
[1,] 504 588
[2,] 588 686
> cov(z)
      [,1] [,2]
[1,] 504 588
[2,] 588 686
> cor(z)
      [,1] [,2]
[1,]    1    1
[2,]    1    1
> sd(z)
[1] 22.44994 26.19160
> z
      [,1] [,2]
[1,]   60   70
[2,]   72   84
[3,]   84   98
[4,]   96  112
[5,]  108  126
[6,]  120  140
```

# Basic stats functions, part 2

# ?cor

```
var(x, y = NULL, na.rm = FALSE, use)

cov(x, y = NULL, use = "everything",
     method = c("pearson", "kendall",
"spearmann"))

cor(x, y = NULL, use = "everything",
     method = c("pearson", "kendall",
"spearmann"))

cov2cor(V)
```

# More on cor

x

a numeric vector, matrix or data frame.

y

NULL (default) or a vector, matrix or data frame with compatible dimensions to x. The default is equivalent to y = x (but more efficient).

na.rm

logical. Should missing values be removed?

use

an optional character string giving a method for computing covariances in the presence of missing values. This must be (an abbreviation of) one of the strings "everything", "all.obs", "complete.obs", "na.or.complete", or "pairwise.complete.obs".

method

a character string indicating which correlation coefficient (or covariance) is to be computed. One of "pearson" (default), "kendall", or "spearman", can be abbreviated.

v

symmetric numeric matrix, usually positive definite such as a covariance matrix.

# row and col as functions

```
> r <- .8
> R <- diag(1,8)
> R
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,]    1    0    0    0    0    0    0    0
[2,]    0    1    0    0    0    0    0    0
[3,]    0    0    1    0    0    0    0    0
[4,]    0    0    0    1    0    0    0    0
[5,]    0    0    0    0    1    0    0    0
[6,]    0    0    0    0    0    1    0    0
[7,]    0    0    0    0    0    0    1    0
[8,]    0    0    0    0    0    0    0    1
> R <- r^(abs(row(R)-col(R)))
> round(R,2)
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] 1.00  0.80  0.64  0.51  0.41  0.33  0.26  0.21
[2,] 0.80  1.00  0.80  0.64  0.51  0.41  0.33  0.26
[3,] 0.64  0.80  1.00  0.80  0.64  0.51  0.41  0.33
[4,] 0.51  0.64  0.80  1.00  0.80  0.64  0.51  0.41
[5,] 0.41  0.51  0.64  0.80  1.00  0.80  0.64  0.51
[6,] 0.33  0.41  0.51  0.64  0.80  1.00  0.80  0.64
[7,] 0.26  0.33  0.41  0.51  0.64  0.80  1.00  0.80
[8,] 0.21  0.26  0.33  0.41  0.51  0.64  0.80  1.00
```

# Yet more stats functions

- I. `sample(n, N, replace=TRUE)`
- II. `eigen(X)` (eigen value decomposition of X)
- III. `solve(X)` (inverse of X)
- IV. `solve (X,Y)` Regression of Y on X

```
> x <- matrix(sample(10,50,replace=TRUE),ncol=5)
> x
```

	[,1]	[,2]	[,3]	[,4]	[,5]
[1, ]	10	3	4	4	6
[2, ]	3	10	8	8	9
[3, ]	1	6	5	8	5
[4, ]	9	1	3	5	3
[5, ]	6	8	3	5	1
[6, ]	8	6	10	1	10
[7, ]	10	5	10	2	1
[8, ]	9	3	2	2	9
[9, ]	6	10	2	9	4
[10, ]	1	8	8	2	6

# Creating a matrix

```
> z <- scale(x)
```

standardize it

```
> z
      [,1]      [,2]      [,3]      [,4]      [,5]
[1,]  1.04838349 -0.9819805 -0.4678877 -0.2059329  0.1852621
[2,] -0.93504473  1.3093073  0.7798129  1.1669533  1.1115724
[3,] -1.50173851  0.0000000 -0.1559626  1.1669533 -0.1235080
...
[9,] -0.08500407  1.3093073 -1.0917380  1.5101749 -0.4322782
[10,] -1.50173851  0.6546537  0.7798129 -0.8923761  0.1852621
attr("scaled:center")
[1] 6.3 6.0 5.5 4.6 5.4
attr("scaled:scale")
[1] 3.529243 3.055050 3.205897 2.913570 3.238655
```

# Just center it

```
> c <- scale(x,scale=FALSE)

> c
     [,1] [,2] [,3] [,4] [,5]
[1,]  3.7   -3  -1.5 -0.6  0.6
[2,] -3.3    4   2.5  3.4  3.6
[3,] -5.3    0  -0.5  3.4 -0.4
[4,]  2.7   -5  -2.5  0.4 -2.4
[5,] -0.3    2  -2.5  0.4 -4.4
[6,]  1.7    0   4.5 -3.6  4.6
[7,]  3.7   -1   4.5 -2.6 -4.4
[8,]  2.7   -3  -3.5 -2.6  3.6
[9,] -0.3    4  -3.5  4.4 -1.4
[10,] -5.3   2   2.5 -2.6  0.6
attr(,"scaled:center")
[1] 6.3 6.0 5.5 4.6 5.4
```

# Find the covariance and inverse

```
> c <- cov(x)
> round(c,2)
      [,1]   [,2]   [,3]   [,4]   [,5]
[1,] 12.46 -6.89 -1.61 -4.53 -1.58
[2,] -6.89  9.33  2.11  4.11  0.56
[3,] -1.61  2.11 10.28 -3.89  2.22
[4,] -4.53  4.11 -3.89  8.49 -1.60
[5,] -1.58  0.56  2.22 -1.60 10.49

> round(solve(c),2)
      [,1]   [,2]   [,3]   [,4]   [,5]
[1,] 0.15  0.08  0.02  0.06  0.02
[2,] 0.08  0.23 -0.07 -0.10  0.00
[3,] 0.02 -0.07  0.16  0.12 -0.01
[4,] 0.06 -0.10  0.12  0.26  0.03
[5,] 0.02  0.00 -0.01  0.03  0.10
```

# Flow control

I. if(condition) {then do this} else {do this}

II. for (condition) do {expression}

A. for (i in 1:n) do {x <- x + 1}

III. while (condition) {expression}

# conditionals

I. (a & b) vs. (a && b)

II. (a | b) vs. (a || b)

```
a <- 1
> if (a & b) {print ("hello")} else {print("goodby")}
Error: object 'b' not found
> if (a && b ) {print ("hello")} else {print("goodby")}
[1] "goodby"
> if (a | b) {print ("hello")} else {print("goodby")}
Error: object 'b' not found

> if (a || b) {print ("hello")} else {print("goodby")}
Error: object 'b' not found
> a <- 1
> if (a || b) {print ("hello")} else {print("goodby")}
[1] "hello"
>
```

# simple control

```
> a <- 1
> b <- 2
> c <- 3
> k <- 10
> x <- 1
> if(x == a) {print("x is the same as a and has
value",x)} else {print ("x is not equal to a")}

> x <- 3
> if(x == a) {print("x is the same as a and has
value",x)} else {print ("x is not equal to a")}
[1] "x is not equal to a"
>
```

# Make that a function

```
> f1 <- function(x,y) {if(x == y) {print  
("x is the same as y and has value",x)}  
else {print ("x is not equal to y")}}  
> f1(3,4)  
[1] "x is not equal to y"  
> f1(5,5)  
[1] "x is the same as y and has value"
```

# Simple functions:part 2

- I. Find the squared multiple correlation of a variable with all the other variables in a matrix.
- II. The  $R^2$  is 1- the residual variance

# The essence of the function

```
SMC <- function(R) {  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)}  
  
> S <- cor(attitude)  
> SMC(S)      #does not show anything  
  
> round(SMC(S),2) #but this does  
                  rating complaints privileges learning      raises  
critical       advance  
               0.73          0.77          0.38          0.62          0.68  
0.19          0.52
```

# Add a return

```
SMC <- function(R) {  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)  
  return(SMC)}  
  
> SMC(S)  
    rating complaints privileges learning      raises  
critical      advance  
 0.7326020  0.7700868  0.3831176  0.6194561  0.6770498  
0.1881465  0.5186447
```

# Allow it to find R

```
SMC <- function(R) {  
  if(dim(R)[1] !=dim(R)[2]) {R <-cor(R)}  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)  
  return(SMC)}
```

```
> SMC(attitude)  
    rating complaints privileges   learning      raises  
critical       advance  
 0.7326020  0.7700868  0.3831176  0.6194561  0.6770498  
0.1881465  0.5186447
```

# Clean up the output

```
SMC <- function(R,digits=2) {  
  if(dim(R)[1] !=dim(R)[2]) {R <- cor(R)}  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)  
  return(round(SMC,digits))}  
  
> SMC(attitude)  
    rating complaints privileges learning      raises critical  
advance  
       0.73        0.77       0.38       0.62       0.68      0.19  
0.52  
>
```

# Check for poor input

```
> att <- data.frame(attitude[1:3],attitude[1:3])
> SMC(att)
Error in solve.default(R) :
  Lapack routine dgesv: system is exactly singular
```

# Add checks for weird matrices

```
SMC <- function(R,digits=2) {  
  p <- dim(R)[2]  
  if (dim(R)[1] != p) {R <- cor(R)}  
  R.inv <- try(solve(R),TRUE)  
  if(class(R.inv)== as.character("try-error")) {SMC <- rep(1,p)  
    warning("Correlation matrix not invertible, smc's returned as 1s")}  
  else {smc <- 1 - 1/diag(R.inv)}  
  SMC <- 1 - 1/diag(R.inv)}  
  return(round(SMC,digits))}  
  
> SMC(att)  
[1] 1 1 1 1 1 1  
Warning message:  
In SMC(att) : Correlation matrix not invertible, smc's returned as  
1s  
  
> SMC(attitude)  
      rating complaints privileges learning      raises critical  
       0.73          0.77         0.38        0.62        0.68        0.19
```

# Further checks

## Input is a covariance matrix

```
> SMC(cov(attitude))  
    rating complaints privileges learning raises critical  
advance  
    -38.62      -39.76     -91.35    -51.42    -33.91    -78.49  
-49.96
```

## Input is raw data or correlations

```
> SMC(cor(attitude))  
    rating complaints privileges learning raises critical  
advance  
    0.73      0.77      0.38      0.62      0.68      0.19  
0.52  
> SMC(attitude)  
    rating complaints privileges learning raises critical  
advance  
    0.73      0.77      0.38      0.62      0.68      0.19  
0.52
```

# Final version

```
#modified Dec 10, 2008 to return 1 on diagonal if non-invertible
#modified March 20, 2009 to return smcs * variance if covariance matrix
is desired
#modified April 8, 2009 to remove bug introduced March 10 when using
covar from data
"smc" <-
function(R,covar =FALSE) {
failed=FALSE
p <- dim(R)[2]
if (dim(R)[1] != p) {if(covar) {C <- cov(R, use="pairwise")
vari <- diag(C)
R <- cov2cor(C)
} else {R <- cor(R,use="pairwise")}}
else {vari <- diag(R)
R <- cov2cor(R)
if (!is.matrix(R)) R <- as.matrix(R)}
R.inv <- try(solve(R),TRUE)
if(class(R.inv)== as.character("try-error")) {smc <- rep(1,p)
warning("Correlation matrix not invertible, smc's returned as 1s")}
else {smc <- 1 -1/diag(R.inv)
if(covar) {smc <- smc * vari}}
return(smc)
}
```

# Creating a new function

- I. Is there a base function to modify?
- II. Consider the case of modifying Promax rotation to allow for any target matrix
- III. original promax (inside the factanal package) had been modified to report the factor correlation.
- IV. This version was created with the assistance of Pat Shrout and Steve Miller

# promax

```
> promax
function (x, m = 4)
{
  if (ncol(x) < 2)
    return(x)
  dn <- dimnames(x)
  xx <- varimax(x)
  x <- xx$loadings
  Q <- x * abs(x)^(m - 1)
  U <- lm.fit(x, Q)$coefficients
  d <- diag(solve(t(U) %*% U))
  U <- U %*% diag(sqrt(d))
  dimnames(U) <- NULL
  z <- x %*% U
  U <- xx$rotmat %*% U
  dimnames(z) <- dn
  class(z) <- "loadings"
  list(loadings = z, rotmat = U)
}
<environment: namespace:stats>
```

```
> Promax
function (x, m = 4)
{
  if (!is.matrix(x) & !is.data.frame(x)) {
    if (!is.null(x$loadings))
      x <- as.matrix(x$loadings)
  }
  else {
    x <- x
  }
  if (ncol(x) < 2)
    return(x)
  dn <- dimnames(x)
  xx <- varimax(x)
  x <- xx$loadings
  Q <- x * abs(x)^(m - 1)
  U <- lm.fit(x, Q)$coefficients
  d <- diag(solve(t(U) %*% U))
  U <- U %*% diag(sqrt(d))
  dimnames(U) <- NULL
  z <- x %*% U
  U <- xx$rotmat %*% U
  ui <- solve(U)
  Phi <- ui %*% t(ui)
  dimnames(z) <- dn
  class(z) <- "loadings"
  result <- list(loadings = z, rotmat = U, Phi = Phi)
  class(result) <- c("psych", "fa")
  return(result)}
```

# Promax

# target.rot

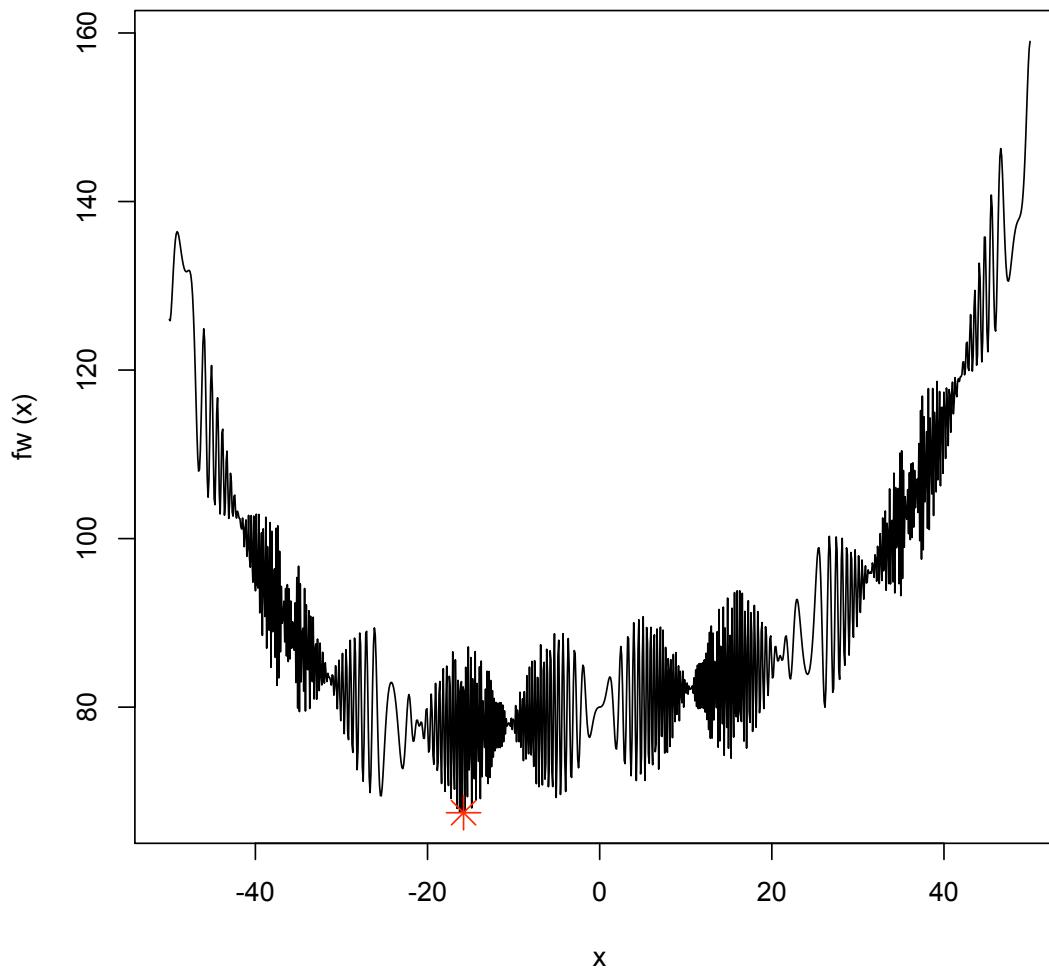
```
"target.rot" <-
function (x, keys=NULL,m = 4)
{
  if(!is.matrix(x) & !is.data.frame(x) )  {
    if(!is.null(x$loadings)) x <- as.matrix(x$loadings)
  } else {x <- x}
  if (ncol(x) < 2)
    return(x)
  dn <- dimnames(x)
  if(is.null(keys)) {xx <- varimax(x)
  x <- xx$loadings
  Q <- x * abs(x)^(m - 1)} else {Q <- keys}
  U <- lm.fit(x, Q)$coefficients
  d <- diag(solve(t(U) %*% U))
  U <- U %*% diag(sqrt(d))
  dimnames(U) <- NULL
  z <- x %*% U
  if (is.null(keys)) {U <- xx$rotmat %*% U } else {U <- U}
  ui <- solve(U)
  Phi <- ui %*% t(ui)
  dimnames(z) <- dn
  class(z) <- "loadings"
  result <- list(loadings = z, rotmat = U,Phi = Phi)
  class(result) <- c("psych","fa")
  return(result)
}
```

# optim as “solver” for R

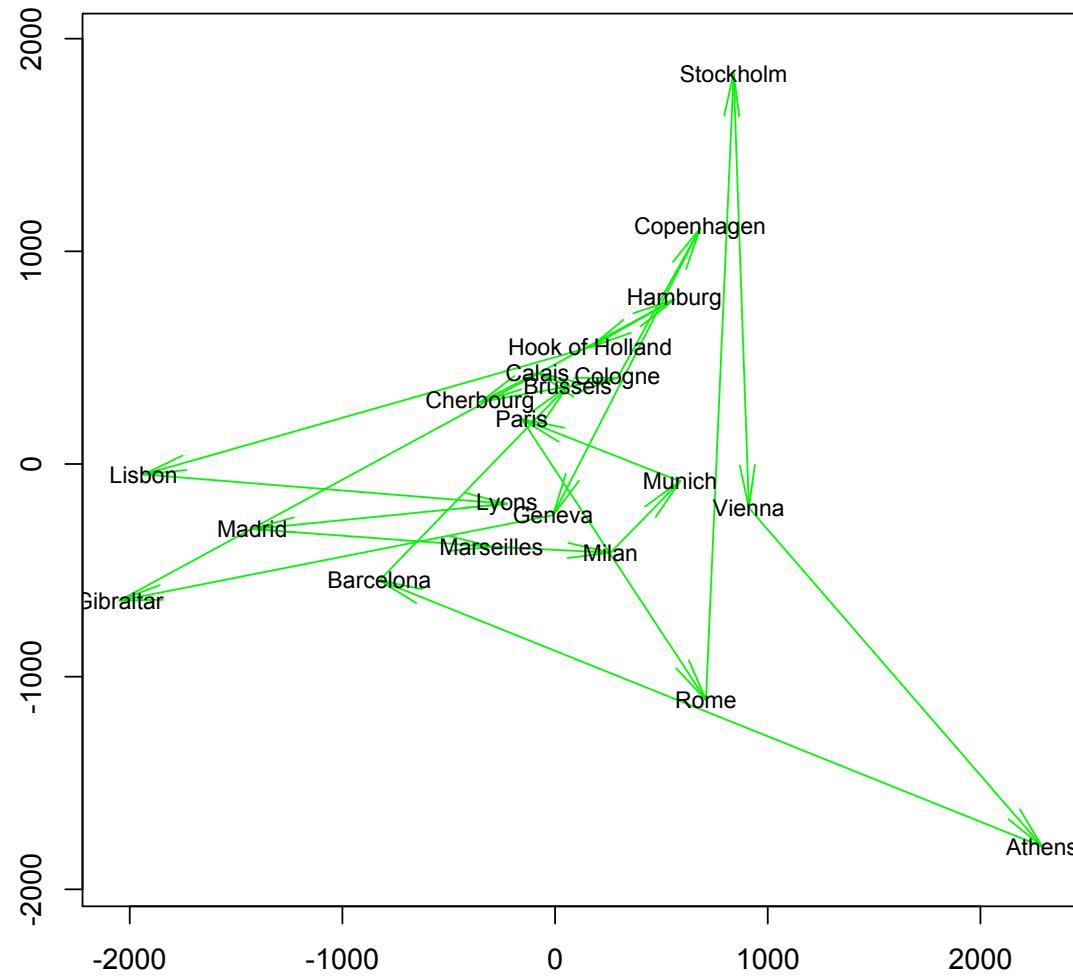
- I. Many statistical functions are not closed form but rather are solved iteratively.
- II. We start with a good guess and then minimize the function
- III. optim will do this for functions where you manipulate one vector (which can of course actually be a matrix)

# optim

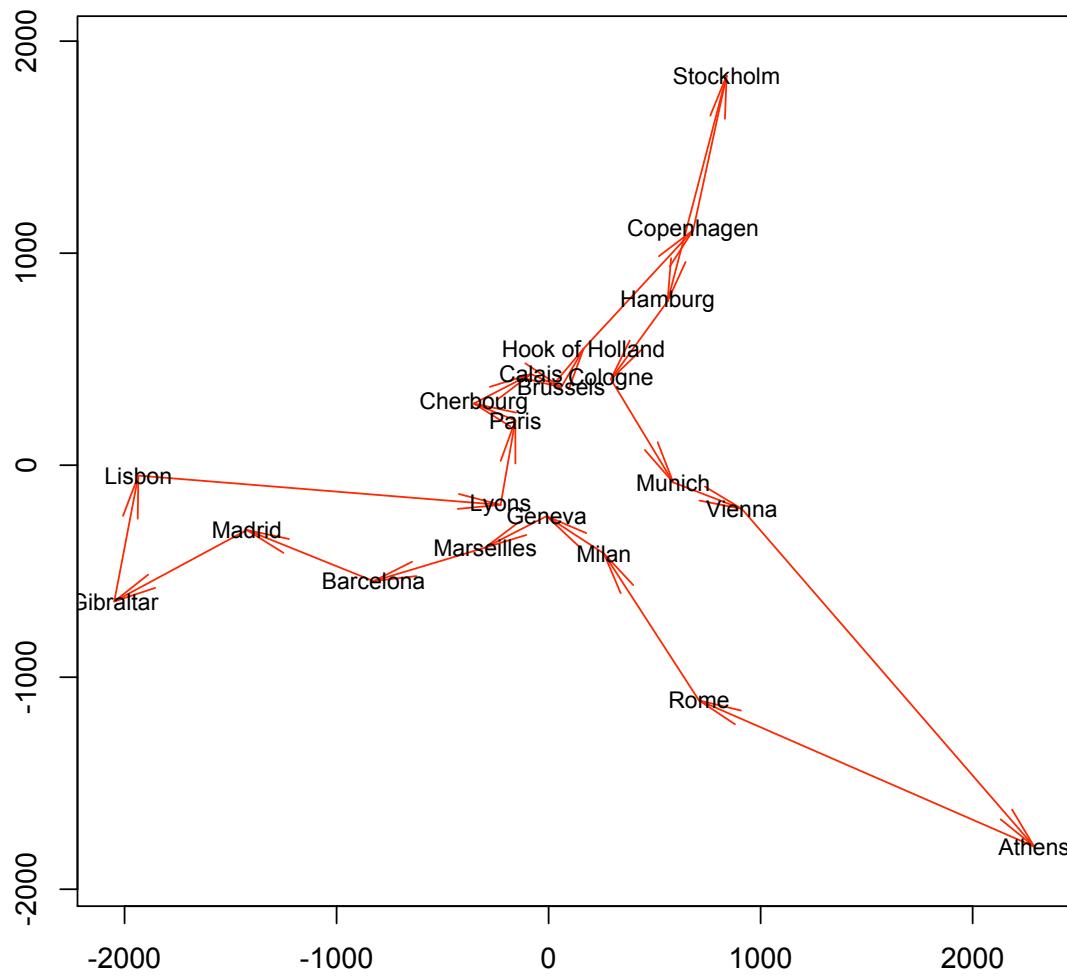
**optim() minimising 'wild function'**



### initial solution of traveling salesman problem



### **optim() 'solving' traveling salesman problem**



# Trying to make a new function to do OLS FA

- I. First, look at current ML FA function
  - A. factanal
  - B. It turns out that the critical optimization is done in factanal.fit.mle, but where is that?
- II. getAnywhere(factanal.fit.mle)
  - A. then look at the code
  - B. scratch your head and try running it

# Sharing your code

- I. Post the source code on your web site
- II. develop a package which you keep on a “repository” on your web site
- III. develop a package and upload it to CRAN

# Package development

- I. a somewhat dated tutorial is found at [http://  
personality-project.org/r/makingpackages.html](http://personality-project.org/r/makingpackages.html)

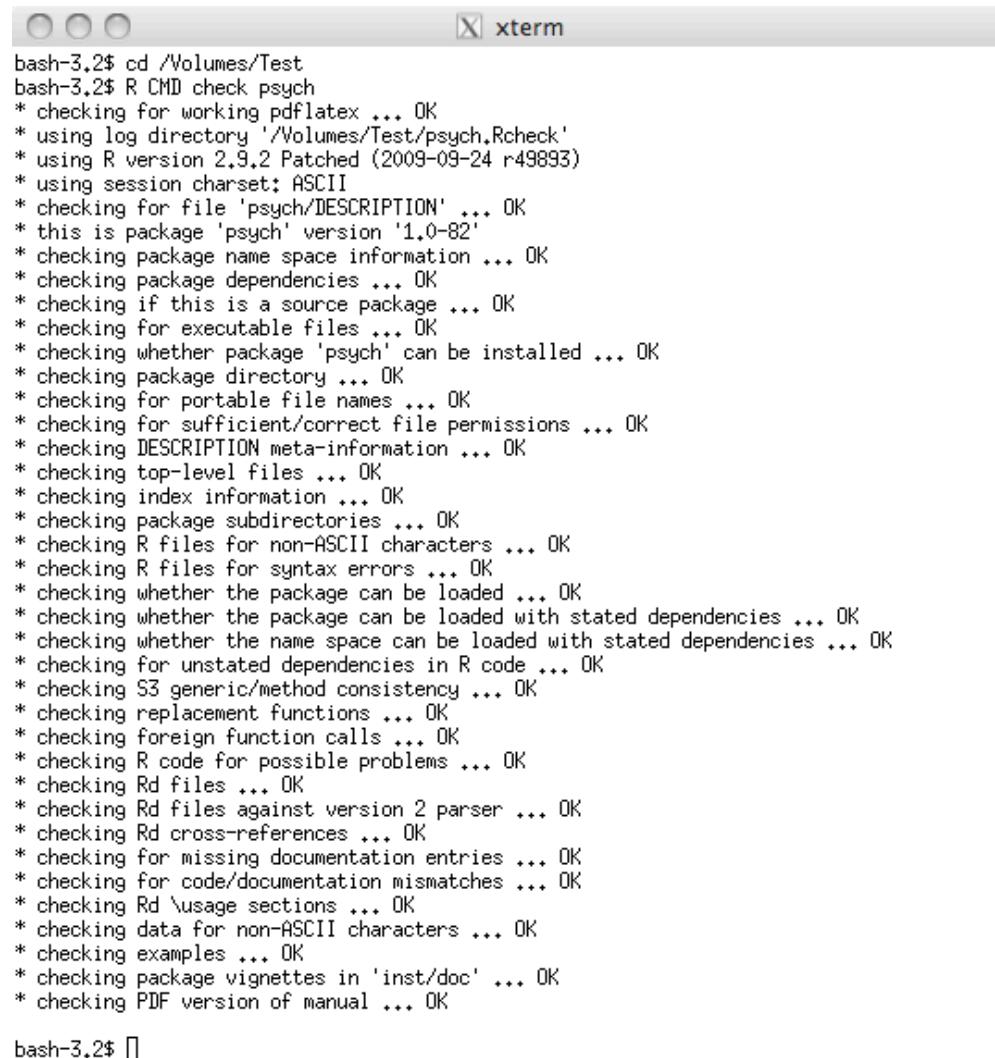
# Package development

- I.package.skeleton(yourpackage) #creates directories and subdirectories for a package
  - A.this includes a number of different subdirectories and files.
- II.prompt(yourfunction) #creates a draft help file for your function
- III.Document as you go

# in X11

- I. R CMD check mypackage #makes sure all the code is correct, checks for matches with documentation, runs all the example,
- II.R CMD make mypackage #builds the package, but does not check except for working R
  - A.this will convert the helpfiles from Rd files to html, LaTeX, and pdf
- III.R CMD install mypackage will add any changes to your current package

# Using X11 to check packages



The image shows a screenshot of an xterm window titled "xterm". The window contains a command-line session where the user is checking the "psych" package. The session starts with the user navigating to a directory and running the R CMD check command. The output shows a series of asterisks (\*) followed by descriptive text and "OK" status indicators, indicating a successful package check. The terminal window has a standard window title bar with three circular icons.

```
bash-3.2$ cd /Volumes/Test
bash-3.2$ R CMD check psych
* checking for working pdflatex ... OK
* using log directory '/Volumes/Test/psych.Rcheck'
* using R version 2.9.2 Patched (2009-09-24 r49893)
* using session charset: ASCII
* checking for file 'psych/DESCRIPTION' ... OK
* this is package 'psych' version '1.0-82'
* checking package name space information ... OK
* checking package dependencies ... OK
* checking if this is a source package ... OK
* checking for executable files ... OK
* checking whether package 'psych' can be installed ... OK
* checking package directory ... OK
* checking for portable file names ... OK
* checking for sufficient/correct file permissions ... OK
* checking DESCRIPTION meta-information ... OK
* checking top-level files ... OK
* checking index information ... OK
* checking package subdirectories ... OK
* checking R files for non-ASCII characters ... OK
* checking R files for syntax errors ... OK
* checking whether the package can be loaded ... OK
* checking whether the package can be loaded with stated dependencies ... OK
* checking whether the name space can be loaded with stated dependencies ... OK
* checking for unstated dependencies in R code ... OK
* checking S3 generic/method consistency ... OK
* checking replacement functions ... OK
* checking foreign function calls ... OK
* checking R code for possible problems ... OK
* checking Rd files ... OK
* checking Rd files against version 2 parser ... OK
* checking Rd cross-references ... OK
* checking for missing documentation entries ... OK
* checking for code/documentation mismatches ... OK
* checking Rd \usage sections ... OK
* checking data for non-ASCII characters ... OK
* checking examples ... OK
* checking package vignettes in 'inst/doc' ... OK
* checking PDF version of manual ... OK

bash-3.2$ []
```

# The structure of a package

▼	psych.Rcheck	Today, 3:16 PM	-- Folder
	psych-manual.pdf	Today, 3:15 PM	1 MB Adobe PDF document
	psych-manual.log	Today, 3:15 PM	70 KB BBEdit text document
	OOcheck.log	Today, 3:15 PM	4 KB BBEdit text document
	psych-Ex.Rout	Today, 3:14 PM	180 KB Document
	psych-Ex.ps	Today, 3:14 PM	6.5 MB PostScript
▼	inst	Today, 3:14 PM	-- Folder
	doc	Today, 3:14 PM	-- Folder
	test.ICLUS graph.dot	Today, 3:13 PM	4 KB Microsoft Word document
	psych-Ex.R	Today, 3:12 PM	70 KB BBEdit text document
	css R.css	Today, 3:12 PM	4 KB CSS style sheet
	OOinstall.out	Today, 3:12 PM	12 KB gmon.out
▼	psych	Today, 3:12 PM	-- Folder
	Meta	Today, 3:12 PM	-- Folder
	INDEX	Today, 3:12 PM	16 KB Document
	doc	Today, 3:12 PM	-- Folder
	R-ex	Today, 3:12 PM	-- Folder
	latex	Today, 3:12 PM	-- Folder
	html	Today, 3:12 PM	-- Folder
	help	Today, 3:12 PM	-- Folder
	CONTENTS	Today, 3:12 PM	25 KB Document
	R	Today, 3:11 PM	-- Folder
	man	Today, 3:11 PM	-- Folder
	NEWS	Today, 3:11 PM	12 KB SimpleText Format
	DESCRIPTION	Today, 3:11 PM	4 KB Document
	data	Today, 3:11 PM	-- Folder
	NAMESPACE	Today, 3:11 PM	4 KB Document

# The package

▼	psych	Aug 28, 2009 11:02 AM	--	Folder
	CHANGES	Oct 5, 2009 9:48 AM	12 KB	SimpleText Format
	DESCRIPTION	Oct 5, 2009 9:48 AM	8 KB	BBEdit text document
►	man	Oct 4, 2009 7:39 PM	--	Folder
	NAMESPACE	Sep 29, 2009 10:04 PM	4 KB	SimpleText Format
►	R	Sep 27, 2009 6:34 PM	--	Folder
	sort.rowcol.R	Aug 28, 2009 11:02 AM	4 KB	BBEdit text document
►	data	Aug 23, 2009 12:31 PM	--	Folder
▼	inst	Jun 30, 2009 7:39 PM	--	Folder
	doc	Yesterday, 2:16 PM	--	Folder
	psych_for_sem.pdf	Yesterday, 2:16 PM	414 KB	Adobe PDF document
	overview.pdf	Yesterday, 2:15 PM	2.3 MB	Adobe PDF document
	psych_for_sem	Sep 30, 2009 9:25 AM	37 KB	Rnw File
	overview	Sep 30, 2009 9:00 AM	66 KB	Rnw File
	psych_manual.pdf	Jul 26, 2009 12:23 PM	1 MB	Adobe PDF document
	all	Jun 30, 2009 7:36 PM	1.5 MB	BibTeX
	apa.bst	Mar 21, 2007 4:33 PM	25 KB	bst File
	NEWS	Sep 30, 2009 7:45 PM	12 KB	SimpleText Format

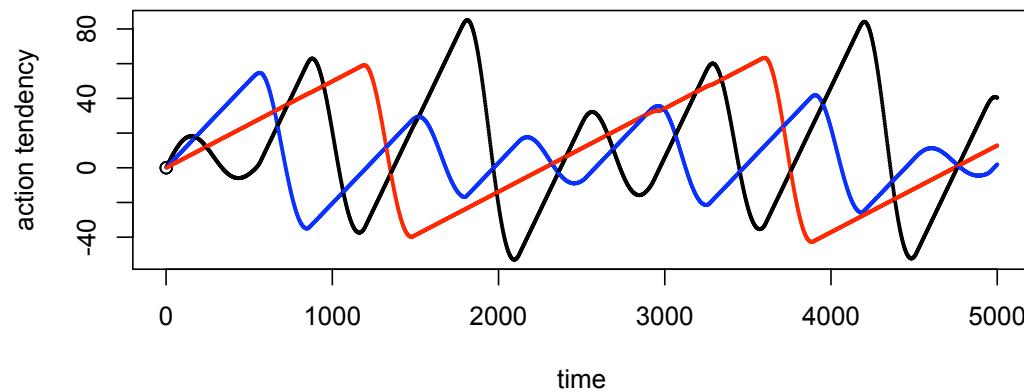
```
mat.sort          text  html  latex example
matrix.addition   text  html  latex example
msq              text  html  latex example
multi.hist        text  html  latex example
neo              text  html  latex example
omega             text  html  latex example
omega.graph      text  html  latex example
p.rep             text  html  latex example
paired.r          text  html  latex example
pairs.panels     text  html  latex example
partial.r         text  html  latex example
peas              text  html  latex example
phi               text  html  latex example
phi.demo          text  html  latex example
phi2poly          text  html  latex example
plot.psych        text  html  latex example
polar              text  html  latex example
poly.mat           text  html  latex example
polychor.matrix   text  html  latex example
principal          text  html  latex example
print.psych        text  html  latex example
r.test             text  html  latex example
read.clipboard    text  html  latex example
rescale            text  html  latex example
sat.act            text  html  latex example
scaling.fits       text  html  latex example
schmid             text  html  latex example
score.alpha        text  html  latex example
score.items        text  html  latex example
score.multiple.choice text  html  latex example
sim               text  html  latex example
sim.VSS            text  html  latex example
sim.anova          text  html  latex example
sim.congeneric    text  html  latex example
sim.hierarchical   text  html  latex example
sim.item            text  html  latex example
sim.structural     text  html  latex example
simulation.circ    text  html  latex example
skew              text  html  latex example
smc               text  html  latex example
structure.graph   text  html  latex example
structure.list     text  html  latex example
super.matrix       text  html  latex example
table2matrix       text  html  latex example
test.psych          text  html  latex example
thurstone          text  html  latex example
tr                 text  html  latex example
vegetables          text  html  latex example
winsor             text  html  latex example
* building package indices ...
` DONE (psych)
` creating vignettes ... OK
` removing junk files
` excluding invalid files from 'psych'
Subdirectory 'R' contains invalid file names:
  correlations neo pearson power reliability.data.sets
` checking for LF line-endings in source and make files
` checking for empty or unneeded directories
` building 'psych_1.0-82.tar.gz'
```

# R CMD build psych

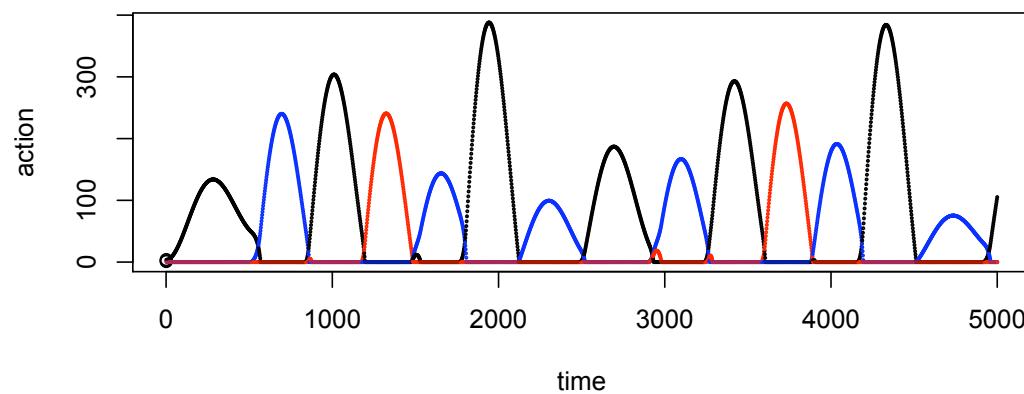
# R in the classroom

- I. Undergraduate statistics and research methods
  - A.describe, pairs.panels, anova, lm
  - B.plot, curve, etc.
  - C.see tutorials for 205 and 371
  - D.simulations of data for simulated studies
  - E.Examples of complex models

**Action Tendencies over time**



**Actions over time**



# R in the classroom

## I. Graduate

- A. data simulations
- B. data analysis
- C. longer tutorial