> Lawrence Hubert

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

Lawrence Hubert

Department of Psychology The University of Illinois

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This talk and the associated handout are at:

cda.psych.uiuc.edu/wallace_handout.pdf

cda.psych.uiuc.edu/wallace_beamer_talk.pdf

What follows is a quote from Studs Terkel, the great oral historian:

There are three great Americans of the 20th century; two are household names, Franklin D. Roosevelt and Martin Luther King. The third should be: Henry A. Wallace.

Henry A. Wallace: A Brief Vita

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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Henry A. Wallace was born in 1888 on a farm in Iowa and into the prominent Wallace family.

His grandfather (Henry Wallace) was the editor and owner of the prominent farm journal, *Wallaces' Farmer*

His father (Henry C. Wallace) worked on the journal; he was also an Associate Professor of Dairy Science at Iowa State, and later the U.S. Secretary of Agriculture from 1921-1924.

Henry A. Wallace:

1910: B.S. in Animal Husbandry, Iowa State College, Ames 1910–1932: Editorial staff of *Wallaces' Farmer* (Chief Editor, 1924–1932) (Motto: Good Farming; Clear Thinking; Right Living)

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1933–1940: U.S. Secretary of Agriculture (under Roosevelt and the New Deal)

1941–1945: Vice-President of the United States (under Roosevelt)

1945–1946: U.S. Secretary of Commerce (under Truman)

1948: Progressive Party nominee for the U.S. Presidency (the Party's platform called for the end of segregation; equal rights for women; and a Medicare-type program [that we will call Wallace-care])

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The Wallace Legacy to Statistical Best Practices

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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Henry A. Wallace demonstrated the best practices in (agricultural) statistics and econometrics throughout his whole life, including his time as the New Deal U.S. Secretary of Agriculture (1933–1940)

Wallace demanded an evidence-based set of agricultural policies and practices (through statistics and data gathering) that helped pull the U.S. out of the Great Depression. He was, for example, the prime initiator of the annual *Agricultural Outlook Report* of the USDA

He is arguably the single individual responsible for the first Department of Statistics in the U.S.; this is due to Wallace's connections with George Snedecor.

He was the lead architect of numerical procedures (in the 1920s) for solving the normal equations in large-scale multiple regression.

Quantitative Training

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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Henry Wallace was self-taught quantitatively and statistically in the decade after he graduated from Iowa State;

he learned most of his statistics from G. Udny Yule's, *An introduction to the theory of statistics* (first edition, 1911); and the possibility of applying statistics to agricultural

problems from H. L. Moore, *Economic Cycles: Their Law and Cause* (1914);

he learned calculus from a book he found in the Des Moines Public Library.

George Washington Carver Influence

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While H.C. Wallace was on the Iowa State faculty, the Wallace family befriended George Washington Carver, the first African-American student at Iowa State College and later an Instructor.

Carver was a botany student and allowed young Henry A. (then about five years old) to accompany him on expeditions in and around Ames.

Henry A. later credited Carver with encouraging his early interest in plants and botany (and I might add, created in Henry A. a life-long interest in the promotion of civil rights).

As a direct quote from Wallace: "George Washington Carver often took me with him on botany expeditions, and it was he who first introduced me to the mysteries of plant fertilization"

Hybrid Corn

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In 1924, Wallace developed a hybrid corn called Copper Cross that won a gold medal at the Iowa Corn Yield Test.

This was the first time a hybrid had beaten standard open pollinated strains.

To market this, Wallace founded in 1926 the (Pioneer) Hi-Bred Corn Company

Slogan: Developed not discovered; Made to fit — not found by chance

By the early 1940s, 98 percent of all planted corn in Iowa (and elsewhere) was hybrid, with much of it sold by Pioneer.

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A small anecdote that shows Wallce's belief in evidence-based actions backed up by statistical analyses (from Mordecai Ezekiel):

During the depths of the depression Wallace built up a market for hybrid seed by offering it to farmers without requiring a cash payment, on condition that they plant half their land in hybrid and half in ordinary corn, and then pay back a fraction of the value of the higher yield on the hybrid acres.

He also encouraged two other companies to go into hybrid seed production and sale, knowing that the potential market was much bigger than his company alone could supply.

Agricultural Prices (Henry A. Wallace; 1920)

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This work has been called the first true econometric study published in the United States.

Wallace commented that economists dealt too much with economic theory and believed that the truth ultimately was to be found in statistics.

Short excepts from the preface and the chapter called the "Technique of the Ratio Method" follow:

Its purpose is to promote a better understanding of the factors which influence prices of farm products and stimulate an intelligent interest in statistical economics.

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If this book is used as a college text, it is hoped that it will be by classes which are especially concerned in applying statistical laws to agricultural prices. Such classes should have free access to calculating machines, multiplying tables, etc., and should make a serious effort to work out various ratios and also to work out supply and demand laws for various farm products by means of correlation coefficients, lines of regression, etc.

TECHNIQUE OF THE RATIO METHOD

The fundamental idea of the ratio method is that the price of every product is determined in the long run by the price of some other product or products. The price of hogs is determined in the long run by the price of corn. ...

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In its simplest form, the ratio method deals with only two products, as for example, with hogs and corn. As an average of the ten Januarys extending from 1907 to 1916, No. 2 corn on the Chicago market sold for 59.9 cents a bushel, and heavy hogs on the same market sold for \$7 per hundredweight. In other words, as an average of this ten-year period, it has required the value of 11.7 bushels of corn to equal in value one hundred pounds of heavy hog flesh.

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The ratio for February is different from the ratio for January, but once a set of ratios is secured for each of the twelve months of the years, it is easily possible to work out charts showing month by month the periods of time when hogs were selling relatively higher than their customary ratio to corn, and when they were selling relatively lower.

[Wallace had devised in 1915 the first hog/corn charts, and published on these extensively in *Wallaces' Farmer*. Wallace is given the primary credit for introducing econometrics to the field of agriculture.]

Corn and Corn-Growing (H.A. Wallace and E.N. Bressman, 1923)

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E.N. Bressman was a graduate student at Iowa State.

This text was a practical guide "written in the language of the farm" and covered everything about corn: botany, breeding, marketing, and sales.

This text went through five editions with the last appearing in 1949.

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Correlation and Machine Calculation (H.A. Wallace and George W. Snedecor; 1925)

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A remarkable publication; its story is told in the handout.

It details how to carry-out Gaussian elimination (using a machine) for the solution of the normal equations when you have many independent variables.

This was Snedecor's first publication (in statistics or elsewhere) at the age of 42.

It led directly to the Mathematical Statistical Service at Iowa State (1927).

And in 1933, to the Iowa State Statistical Laboratory, arguably the first "Department of Statistics" in the United States.

In some reminiscences made in 1951 at the Oral History Research Office of Columbia University, Wallace comments:

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My work on cycles began in about 1913, when I began to study the relationship of weather to corn yields, of corn supply to corn prices, the relation of corn prices to hog prices, the cycle of hogs, the cycle of cattle, the cycle of horses, and so on. I did that as a preliminary to getting into more serious and careful statistical work. As a result of studying the relationship of corn weather to corn yields, I ran across the work of H.L. Moore, the Columbia University professor. He had put out some very careful statistical analyses involving the relation of independent variables to a dependent variable, expressing them by regression lines and correlation coefficients. Suffice it to say that I became proficient at doing work of that kind, using a key-driven calculating machine to facilitate matters.

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I thought that the people at the Iowa State College of Agriculture and Mechanical Arts at Ames were not sufficiently current in that field. I went up and met with several of the professors and sold them on the idea that they should be able to evaluate their experimental work much more accurately if they had more adequate statistical background. As a result, they employed me for ten weeks to conduct a statistical course ... There was no one in the class of some twenty who was not

either a professor or a post-graduate student.

Wallace continues:

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Then I took another problem which was interesting to them as agricultural people-the relationship between farm land values in the different counties-for which there were census figures-and the yield of corn per acre. We used an average of ten years for which we had crop reporting figures. We used the percentage of the crop land in corn, for which we had census figures; the value of the buildings per acre, for which we had census figures; and so on. We took up various independent variables bearing on the dependent variable of the value of the farm land per acre. That was the problem which I set to them, which later was embodied in a bulletin put out by Iowa State College entitled Correlation and Machine Calculation.

Other Notable Occurrences at Iowa State

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Noting that H.A. Wallace was head of the USDA from 1933 to 1940, we may have the literal as well as figurative giving of "pork" to Iowa State Statistics.

The Statistics Section of the Iowa Agricultural Experiment Station was organized in 1935, with Snedecor as Section Head.

A hugely lucrative cooperative agreement was made in 1938 between Iowa State and the USDA for joint research in agricultural statistics and related statistical theory:

survey methodology for area sampling and the development of the Master Sample of Agriculture;

methods for forecasting and estimating crop yields.

What's Looks to a Hog (H.A. Wallace, Wallaces' Farmer, 1907)

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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"Corn shows" were very popular at the turn of the century, with major prizes given for the appearance of corn.

As a teenager (16 years old), Wallace test-planted five acres with corn from the "Corn Professor," Perry Holden, that had been judged for "beauty." [Wallace had been experimenting with plant breeding in his own plot since he was ten.]

After meticulous quantitative analysis of the test-planting, Wallace found no correlation between beauty and high yield.

An instance of "what you see is not what you get."

As a result of Wallace's work (and writing about it in *Wallaces' Farmer*), corn shows were gradually replaced by yield contests.

This is a good example where a "surrogate end point" (i.e., corn beauty) is not a good one for the real endpoint of interest (i.e., corn yield).

Corn and Its Early Fathers (Henry A. Wallace and William L. Brown)

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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William L. Brown was the Chairman and President of Pioneer Hi-Bred International, the company Wallace founded in 1926. There are two editions of this book; one in 1956 and a second in 1988 after Wallace had died.

Brown revised this text to reflect the contributions of Wallace to the corn story; and to specifically highlight the fact that Wallace's work with corn was part of the worldwide agricultural revolution initiated by Wallace.

There is a remarkable Chapter 14, Small Gardens and Big Ideas, that is given in the handout. A few quotes are given from this chapter:

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More and more, we feel that grave danger exists of statistics being used as a substitute for critical observation and thought. The senior author joins somewhat apologetically in presenting this point of view because he had a lot to do, back in 1923, with starting the present Statistical Laboratory in Iowa State College, one of the better departments of its kind in the nation. Statistics have their place, a very important one, but they can never serve as a substitute for close association with plants. Their real value, it seems to us, is in measuring precisely what we already know in a general way. Statistics tends to be an office art based on machines and figures rather than a field art based on living things.

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A great deal of work has gone into the development of mathematical models designed to explain just how hybrid vigor operates. As a mode of attack, we believe, it overlooks completely the more important problem of understanding the specific ways in which hybrid vigor affects the plant itself. We fear that until we return to thinking of corn in terms of what the plant itself is doing, instead of working out neat mathematical formulae to fit what we think its performance should be, no real advance will be made.

What is in the corn judge's mind?

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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This is a highly cited paper (H.A. Wallace, *Journal of the American Society of Agronomy*, 1923) in the contemporary judgement and decision-making literature; it is reproduced in whole in the handout.

[There is also an article by H.A. Wallace in *Wallaces' Farmer* (March 2, 1923) that tells the story to farmers without actually using the solutions to the normal equations (*What the Corn Judge Can't See*: Factors that Determine Yield Don't Show on the Score Card).]

It may be the first empirical piece to appear anywhere on the distinction between "Actuarial versus Clinical Prediction."

It relies on Sewall Wright's method of path coefficients published in 1921 as "Correlation and Causation"

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In the form that Wallace used Sewall's method, he had 500 ears of corn that were assessed using six (independent) variables:

- b: length (ear)
- c: circumference (ear)
- d: weight of kernel
- e: filling of kernel at tip
- f: absence of blistering
- g: absence of starchiness

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There were two possible dependent variables:

- a: judge's rating
- y: yield (field tested)

The intercorrelation matrix follows:

	а	b	С	d	е	f	g	у
а	х	.7	.4	.5	.4	.2	.3	.2
b	.7	х	.3	.3	.2	.2	.2	.2
с	.4	.3	х	.2	.1	.0	.0	.15
d	.5	.3	.2	х	.4	.2	.2	.4
е	.4	.2	.1	.4	х	.5	.6	.4
f	.2	.2	.0	.2	.5	х	.5	.3
g	.3	.2	.0	.2	.6	.5	х	.2
у	.2	.2	.15	.4	.3	.2	.2	х

Matlab corn_script.m

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rater_vector = [.7;.4;.5;.4;.2;.3] $vield_vector = [.2:.15:.4:.3:.2:.2]$ intercorr = [1.0 .3 .3 .2 .2 .2; .3 1.0 .2 .1 .0 .0;3 .2 1.0 .4 .2 .2; .2 .1 .4 1.0 .5 .6; .2 .0 .2 .5 1.0 .5;2.0.2.6.51.0] beta_rater = inv(intercorr)* rater_vector $beta_rater_abs = abs(beta_rater)$ $sum_beta_rater = sum(beta_rater_abs)$ prop_beta_rater = (beta_rater_abs) ./ (sum_beta_rater) $beta_yield = inv(intercorr)^*$ yield_vector $beta_yield_abs = abs(beta_yield)$ $sum_beta_yield = sum(beta_yield_abs)$ $prop_beta_vield = (beta_vield_abs) . / (sum_beta_vield)$ rsquared_rater = (rater_vector')*beta_rater $rsquared_vield = (vield_vector')*beta_vield$

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beta_rater =
0.5437 0.1730 0.2334 0.1726 -0.0830 0.0825
sum beta rater =
1.2881
prop_beta_rater =
0.4221 0.1343 0.1812 0.1340 0.0644 0.0641
beta_yield =
0.0480 0.0623 0.3105 0.1123 0.0556 0.0331
sum_beta_yield =
0.6218
prop_beta_yield =
0.0771 0.1002 0.4994 0.1806 0.0894 0.0533
rsquared_rater =
0.6436
rsquared_yield =
0.1946
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Policies as U.S. Secretary of Agriculture During the New Deal

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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The U.S. was in the depths of the Depression when Roosevelt took office in 1933; much of the New Deal rested on policies that Wallace propounded and that eventually helped stabilize U.S. agriculture and put the U.S. on a course out of the depression.

Within less than 100 days of taking office, Wallace had devised ways of controlling production and conserving the soil at the same time; this revolutionary system of supplementing farm income came in exchange for cutting back on production:

A fourth of the nation's cotton crop was plowed under; six million baby piglets were destroyed

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At the same time, government brought electricity to farms, hot lunches to needy children, and food stamps to the poor. To protect the soil, the Department of Agriculture created Shelter Belts-barriers to soil-robbing winds that still stand today; the USDA encouraged farmers to build terraces to reduce water erosion and paid them to take their most vulnerable acres out of production.

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Ever-Normal Granary History

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To ease the ups and downs of the food supply cycle, Wallace created a storehouse system he called the "ever-normal granary"

Price-stabilizing granaries were first established in the 1st century BC.

Under the Qing dynasty they were set up by all Chinese provinces in each county to keep grain on hand to offset regional food shortages in years of crop failure.

By keeping the supply of grain stable ("ever normal"), the granaries stabilized prices, and even undeveloped regions of the country were protected from famine.

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The "ever-normal granary" form of buffer stock has been instituted in the Western world since at least biblical times; in Genesis, the Egyptians used an ever-normal granary to stabilize their food market during the seven years of high yields and subsequent seven years of famine (Joseph was in charge).

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A Few Notable People at the USDA During Wallace's Tenure

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John Kenneth Galbraith worked at the USDA on New Deal initiatives (Berkeley Ph.D. in Agricultural Economics, 1934) Mordecai Ezekial worked as the Economic Advisor to the Secretary of Agriculture (published *Methods of Correlation Analysis*, 1930; 1941). Speaking of Wallace, he said:

He was one of the great generative forces of the first half of the twentieth century.

Adlai Stevenson worked for the Agricultural Adjustment Administration.

W. Edwards Deming worked at the USDA (1928–1938); he brought Walter Shewhart to lecture (and brought his ideas to the 1940 census)

Deming brought Neyman to the USDA Graduate School to lecture in 1937; this led to *Lectures and conferences on mathematical statistics and probability* (1938; 1952)

"Assistant President," 1940–1944

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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As Roosevelt's Vice President, Wallace took on so many tasks that he was referred to as "Assistant President"

As the only scientist in the cabinet, Wallace headed the top secret committee that made the final recommendation to proceed with building the atomic bomb.

Wallace was in charge of the U.S. Board of Economic Warfare that was set up right before the entry of the U.S. into World War II.

After attending the inauguration to the new President of Mexico in 1940, he remained in the country for six weeks assessing Mexican agriculture. Appalled by its primitive condition, Wallace petitioned the Rockefeller Foundation to fund the first international agricultural research station. They did, and this started the worldwide "green revolution"

Norman Borlaug

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The person who was chosen to head this research station was lowan Norman Borlaug who won the Nobel Peace Prize in 1970 for his work in developing disease-resistant wheat.

From Wikipedia:

Norman Ernest Borlaug (2014–2009) was an American agronomist, humanitarian and Nobel laureate who has been called "the father of the Green Revolution," "agriculture's greatest spokesperson" and "The Man Who Saved A Billion Lives." He is one of seven people to have won the Nobel Peace Prize, the Presidential Medal of Freedom and the Congressional Gold Medal; he was also awarded the Padma Vibhushan, India's second highest civilian honor.

Borlaug received his Ph.D. in plant pathology and genetics from the University of Minnesota in 1942. He took up an agricultural research position in Mexico, where he developed semi-dwarf, high-yield, disease-resistant wheat varieties.

Two Structures Named for Henry A. Wallace

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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The Henry A. Wallace Beltsville Agricultural Research Center-the largest agricultural research complex in the world.

The Henry A. Wallace (seminar) Room in the Department of Statistics at Iowa State University–which proudly displays his portrait.

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Other Notable Facts

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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Almost fifty percent of the world's eggs are produced by hens that derive from the genetics of Hy-Line poultry stock;

the Hy-Line breed was developed by Wallace in the 1930s; the company was founded in 1936.

Pioneer Hi-bred is now wholly owned by Dupont; it was bought in 1999 for 10 Billion dollars.

During R.A. Fisher's visit to the U.S. and Iowa State in the Summer of 1931, Henry Wallace attended most of Fisher's lectures; word has it however that Fisher was not particularly interested in Wallace's more fanciful ideas, i.e., the placement of the planets and weather in Iowa, and how that all affects corn production.

Items Present in the Handout

Henry A. Wallace (1888–1965): Agricultural Statistician (Econometrician) Extraordinaire

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1) Journal of the American Society of Agronomy, 1923, 15, 300–304.

WHAT IS IN THE CORN JUDGE'S MIND?

2) Henry Wallace and statistics by Oscar Kempthorne

3) Henry A. Wallace and the Modeling of Expert Judgments (From *A Statistical Guide for the Ethically Perplexed*, Lawrence Hubert and Howard Wainer, 2013, pp. 146–150).

4) corn_script.m and results

5) From *Correlation and Machine Calculation*, Wallace and Snedecor, Part VI: Precautions and Suggestions (1925, pp. 46–47)

6) Excerpt from H.A. David, *Statistics in U.S. Universities in* 1933 and the Establishment of the Statistical Laboratory at Iowa State, Statistical Science, 1998, 13, 66–74.

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7) From John C. Culver and John Hyde, *American Dreamer: A Life of Henry A. Wallace*, 2000, pp. 26–29

8) Corn and Its Early Fathers (Henry A. Wallace and William L. Brown; 1956 and 1988); Chapter 14: Small Gardens and Big Ideas

9) The Story of a Perplexing and Indomitably Naive Public Servant

AMERICAN DREAMER: The Life and Times of Henry A. Wallace; By John C. Culver and John Hyde; W.W. Norton (2000).

March 12, 2000 — ARTHUR SCHLESINGER JR. —

10) *Early Statistics at Iowa State University*, Jay L. Lush, Chapter 5: The Wallace Lectures

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